



King's Research Portal

DOI:

[10.1103/PhysRevLett.118.221101](https://doi.org/10.1103/PhysRevLett.118.221101)

Document Version

Publisher's PDF, also known as Version of record

[Link to publication record in King's Research Portal](#)

Citation for published version (APA):

LIGO Scientific Collaboration, & VIRGO Collaboration (2017). GW170104: Observation of a 50-Solar-Mass Binary Black Hole Coalescence at Redshift 0.2. *Phys. Rev. Lett.*, 118, [221101]. DOI: 10.1103/PhysRevLett.118.221101

Citing this paper

Please note that where the full-text provided on King's Research Portal is the Author Accepted Manuscript or Post-Print version this may differ from the final Published version. If citing, it is advised that you check and use the publisher's definitive version for pagination, volume/issue, and date of publication details. And where the final published version is provided on the Research Portal, if citing you are again advised to check the publisher's website for any subsequent corrections.

General rights

Copyright and moral rights for the publications made accessible in the Research Portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognize and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the Research Portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the Research Portal

Take down policy

If you believe that this document breaches copyright please contact librarypure@kcl.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.



GW170104: Observation of a 50-Solar-Mass Binary Black Hole Coalescence at Redshift 0.2

B. P. Abbott *et al.**

(LIGO Scientific and Virgo Collaboration)

(Received 9 May 2017; published 1 June 2017)

We describe the observation of GW170104, a gravitational-wave signal produced by the coalescence of a pair of stellar-mass black holes. The signal was measured on January 4, 2017 at 10:11:58.6 UTC by the twin advanced detectors of the Laser Interferometer Gravitational-Wave Observatory during their second observing run, with a network signal-to-noise ratio of 13 and a false alarm rate less than 1 in 70 000 years. The inferred component black hole masses are $31.2^{+8.4}_{-6.0} M_{\odot}$ and $19.4^{+5.3}_{-5.9} M_{\odot}$ (at the 90% credible level). The black hole spins are best constrained through measurement of the effective inspiral spin parameter, a mass-weighted combination of the spin components perpendicular to the orbital plane, $\chi_{\text{eff}} = -0.12^{+0.21}_{-0.30}$. This result implies that spin configurations with both component spins positively aligned with the orbital angular momentum are disfavored. The source luminosity distance is 880^{+450}_{-390} Mpc corresponding to a redshift of $z = 0.18^{+0.08}_{-0.07}$. We constrain the magnitude of modifications to the gravitational-wave dispersion relation and perform null tests of general relativity. Assuming that gravitons are dispersed in vacuum like massive particles, we bound the graviton mass to $m_g \leq 7.7 \times 10^{-23}$ eV/ c^2 . In all cases, we find that GW170104 is consistent with general relativity.

DOI: [10.1103/PhysRevLett.118.221101](https://doi.org/10.1103/PhysRevLett.118.221101)

I. INTRODUCTION

The first observing run of the Advanced Laser Interferometer Gravitational-Wave Observatory (LIGO) [1] identified two binary black hole coalescence signals with high statistical significance, GW150914 [2] and GW151226 [3], as well as a less significant candidate LVT151012 [4,5]. These discoveries ushered in a new era of observational astronomy, allowing us to investigate the astrophysics of binary black holes and test general relativity (GR) in ways that were previously inaccessible [6,7]. We now know that there is a population of binary black holes with component masses $\gtrsim 25 M_{\odot}$ [5,6], and that merger rates are high enough for us to expect more detections [5,8].

Advanced LIGO's second observing run began on November 30, 2016. On January 4, 2017, a gravitational-wave signal was detected with high statistical significance. Figure 1 shows a time-frequency representation of the data from the LIGO Hanford and Livingston detectors, with the signal GW170104 visible as the characteristic chirp of a binary coalescence. Detailed analyses demonstrate that GW170104 arrived at Hanford ~ 3 ms before Livingston, and originated from the coalescence of two stellar-mass black holes at a luminosity distance of $\sim 3 \times 10^9$ light-years.

*Full author list given at the end of the Letter.

Published by the American Physical Society under the terms of the [Creative Commons Attribution 4.0 International](https://creativecommons.org/licenses/by/4.0/) license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI.

GW170104's source is a heavy binary black hole system, with a total mass of $\sim 50 M_{\odot}$, suggesting formation in a subsolar metallicity environment [6]. Measurements of the black hole spins show a preference away from being (positively) aligned with the orbital angular momentum, but do not exclude zero spins. This is distinct from the case for GW151226, which had a strong preference for spins with positive projections along the orbital angular momentum [3]. The inferred merger rate agrees with previous calculations [5,8], and could potentially be explained by binary black holes forming through isolated binary evolution or dynamical interactions in dense stellar clusters [6].

Gravitational-wave observations of binary black holes are the ideal means to test GR and its alternatives. They provide insight into regimes of strong-field gravity where velocities are relativistic and the spacetime is dynamic. The tests performed with the sources detected in the first observing run showed no evidence of departure from GR's predictions [5,7]; GW170104 provides an opportunity to tighten these constraints. In addition to repeating tests performed in the first observing run, we also test for modifications to the gravitational-wave dispersion relation. Combining measurements from GW170104 with our previous results, we obtain new gravitational-wave constraints on potential deviations from GR.

II. DETECTORS AND DATA QUALITY

The LIGO detectors measure gravitational-wave strain using two dual-recycled Fabry-Perot Michelson interferometers at the Hanford and Livingston observatories [1,10].

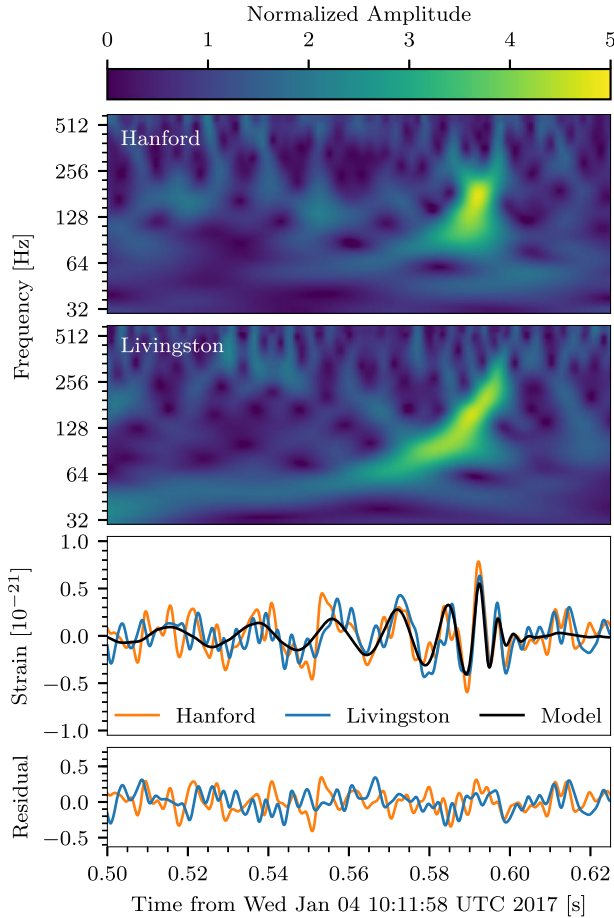


FIG. 1. Time–frequency representation [9] of strain data from Hanford and Livingston detectors (top two panels) at the time of GW170104. The data begin at 1167559936.5 GPS time. The third panel from the top shows the time-series data from each detector with a 30–350 Hz bandpass filter, and band-reject filters to suppress strong instrumental spectral lines. The Livingston data have been shifted back by 3 ms to account for the source’s sky location, and the sign of its amplitude has been inverted to account for the detectors’ different orientations. The maximum-likelihood binary black hole waveform given by the full-precession model (see Sec. IV) is shown in black. The bottom panel shows the residuals between each data stream and the maximum-likelihood waveform.

After the first observing run, both LIGO detectors underwent commissioning to reduce instrumental noise, and to improve duty factor and data quality (see Sec. I in the Supplemental Material [11]). For the Hanford detector, a high-power laser stage was introduced, and as the first step the laser power was increased from 22 to 30 W to reduce shot noise [10] at high frequencies. For the Livingston detector, the laser power was unchanged, but there was a significant improvement in low-frequency performance mainly due to the mitigation of scattered light noise.

Calibration of the interferometers is performed by inducing test-mass motion using photon pressure from modulated calibration lasers [12,13]. The one-sigma

calibration uncertainties for strain data in both detectors for the times used in this analysis are better than 5% in amplitude and 3° in phase over the frequency range 20–1024 Hz.

At the time of GW170104, both LIGO detectors were operating with sensitivity typical of the observing run to date and were in an observation-ready state. Investigations similar to the detection validation procedures for previous events [2,14] found no evidence that instrumental or environmental disturbances contributed to GW170104.

III. SEARCHES

GW170104 was first identified by inspection of low-latency triggers from Livingston data [15–17]. An automated notification was not generated as the Hanford detector’s calibration state was temporarily set incorrectly in the low-latency system. After it was manually determined that the calibration of both detectors was in a nominal state, an alert with an initial source localization [18,19] was distributed to collaborating astronomers [20] for the purpose of searching for a transient counterpart. About 30 groups of observers covered the parts of the sky localization using ground- and space-based instruments, spanning from γ ray to radio frequencies as well as high-energy neutrinos [21].

Offline analyses are used to determine the significance of candidate events. They benefit from improved calibration and refined data quality information that is unavailable to low-latency analyses [5,14]. The second observing run is divided into periods of two-detector cumulative coincident observing time with $\gtrsim 5$ days of data to measure the false alarm rate of the search at the level where detections can be confidently claimed. Two independently designed matched filter analyses [16,22] used 5.5 days of coincident data collected from January 4, 2017 to January 22, 2017.

These analyses search for binary coalescences over a range of possible masses and by using discrete banks [23–28] of waveform templates modeling binaries with component spins aligned or antialigned with the orbital angular momentum [29]. The searches can target binary black hole mergers with detector-frame total masses $2M_\odot \leq M^{\text{det}} \lesssim 100\text{--}500M_\odot$, and spin magnitudes up to ~ 0.99 . The upper mass boundary of the bank is determined by imposing a lower limit on the duration of the template in the detectors’ sensitive frequency band [30]. Candidate events must be found in both detectors by the same template within 15 ms [4]. This 15-ms window is determined by the 10-ms intersite propagation time plus an allowance for the uncertainty in identified signal arrival times of weak signals. Candidate events are assigned a detection statistic value ranking their relative likelihood of being a gravitational-wave signal: the search uses an improved detection statistic compared to the first observing run [31]. The significance of a candidate event is calculated by comparing its detection statistic value to an estimate of the background noise [4,16,17,22]. GW170104 was detected

with a network matched-filter signal-to-noise ratio (SNR) of 13. At the detection statistic value assigned to GW170104, the false alarm rate is less than 1 in 70 000 years of coincident observing time.

The probability of astrophysical origin P_{astro} for a candidate event is found by comparing the candidate's detection statistic to a model described by the distributions and rates of both background and signal events [8,32,33]. The background distribution is analysis dependent, being derived from the background samples used to calculate the false alarm rate. The signal distribution can depend on the mass distribution of the source systems; however, we find that different models of the binary black hole mass distribution (as described in Sec. VI) lead to negligible differences in the resulting value of P_{astro} . At the detection statistic value of GW170104, the background rate in both matched filter analyses is dwarfed by the signal rate, yielding $P_{\text{astro}} > 1 - (3 \times 10^{-5})$.

An independent analysis that is not based on matched filtering, but instead looks for generic gravitational-wave bursts [2,34] and selects events where the signal frequency rises over time [35], also identified GW170104. This approach allows for signal deviations from the waveform models used for matched filtering at the cost of a lower significance for signals that are represented by the considered templates. This analysis reports a false alarm rate of ~ 1 in 20 000 years for GW170104.

IV. SOURCE PROPERTIES

The source parameters are inferred from a coherent Bayesian analysis of the data from both detectors [36,37]. As a cross-check, we use two independent model-waveform families. Both are tuned to numerical-relativity simulations of binary black holes with nonprecessing spins, and introduce precession effects through approximate prescriptions. One model includes inspiral spin precession using a single effective spin parameter χ_p [38–40]; the other includes the generic two-spin inspiral precession dynamics [41–43]. We refer to these as the effective-precession and full-precession models, respectively [44]. The two models yield consistent results. Table I shows selected source parameters for GW170104; unless otherwise noted, we quote the median and symmetric 90% credible interval for inferred quantities. The final mass (or equivalently the energy radiated), final spin, and peak luminosity are computed using averages of fits to numerical-relativity results [45–49]. The parameter uncertainties include statistical and systematic errors from averaging posterior probability distributions over the two waveform models, as well as calibration uncertainty [37] (and systematic uncertainty in the fit for peak luminosity). Statistical uncertainty dominates the overall uncertainty as a consequence of the moderate SNR.

For binary coalescences, the gravitational-wave frequency evolution is primarily determined by the component masses. For higher mass binaries, merger and ringdown dominate the

TABLE I. Source properties for GW170104: median values with 90% credible intervals. We quote source-frame masses; to convert to the detector frame, multiply by $(1+z)$ [50,51]. The redshift assumes a flat cosmology with Hubble parameter $H_0 = 67.9 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and matter density parameter $\Omega_m = 0.3065$ [52]. More source properties are given in Table I of the Supplemental Material [11].

Primary black hole mass m_1	$31.2^{+8.4}_{-6.0} M_\odot$
Secondary black hole mass m_2	$19.4^{+5.3}_{-5.9} M_\odot$
Chirp mass \mathcal{M}	$21.1^{+2.4}_{-2.7} M_\odot$
Total mass M	$50.7^{+5.9}_{-5.0} M_\odot$
Final black hole mass M_f	$48.7^{+5.7}_{-4.6} M_\odot$
Radiated energy E_{rad}	$2.0^{+0.6}_{-0.7} M_\odot c^2$
Peak luminosity ℓ_{peak}	$3.1^{+0.7}_{-1.3} \times 10^{56} \text{ erg s}^{-1}$
Effective inspiral spin parameter χ_{eff}	$-0.12^{+0.21}_{-0.30}$
Final black hole spin a_f	$0.64^{+0.09}_{-0.20}$
Luminosity distance D_L	$880^{+450}_{-390} \text{ Mpc}$
Source redshift z	$0.18^{+0.08}_{-0.07}$

signal, allowing good measurements of the total mass $M = m_1 + m_2$ [53–57]. For lower mass binaries, like GW151226 [3], the inspiral is more important, providing precision measurements of the chirp mass $\mathcal{M} = (m_1 m_2)^{3/5} / M^{1/5}$ [58–61]. The transition between the regimes depends upon the detectors' sensitivity, and GW170104 sits between the

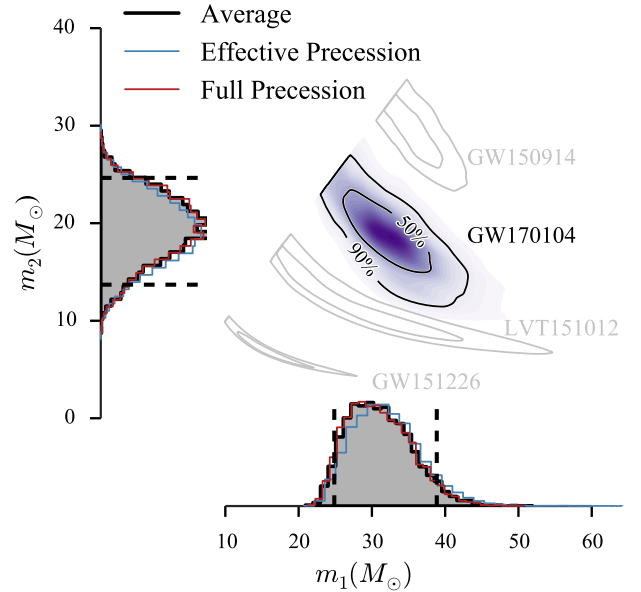


FIG. 2. Posterior probability density for the source-frame masses m_1 and m_2 (with $m_1 \geq m_2$). The one-dimensional distributions include the posteriors for the two waveform models, and their average (black). The dashed lines mark the 90% credible interval for the average posterior. The two-dimensional plot shows the contours of the 50% and 90% credible regions plotted over a color-coded posterior density function. For comparison, we also show the two-dimensional contours for the previous events [5].

two. The inferred component masses are shown in Fig. 2. The form of the two-dimensional distribution is guided by the combination of constraints on M and \mathcal{M} . The binary was composed of two black holes with masses $m_1 = 31.2^{+8.4}_{-6.0} M_\odot$ and $m_2 = 19.4^{+5.3}_{-5.9} M_\odot$; these merged into a final black hole of mass $48.7^{+5.7}_{-4.6} M_\odot$. This binary ranks second, behind GW150914's source [5,37], as the most massive stellar-mass binary black hole system observed to date.

The black hole spins play a subdominant role in the orbital evolution of the binary, and are more difficult to determine. The orientations of the spins evolve due to precession [62,63], and we report results at a point in the inspiral corresponding to a gravitational-wave frequency of 20 Hz [37]. The effective inspiral spin parameter $\chi_{\text{eff}} = (m_1 a_1 \cos \theta_{LS_1} + m_2 a_2 \cos \theta_{LS_2})/M$ is the most important spin combination for setting the properties of the inspiral [64–66] and remains important through to merger [67–71]; it is approximately constant throughout the orbital evolution [72,73]. Here $\theta_{LS_i} = \cos^{-1}(\hat{\mathbf{L}} \cdot \hat{\mathbf{S}}_i)$ is the tilt angle between the spin \mathbf{S}_i and the orbital angular momentum \mathbf{L} , which ranges from 0° (spin aligned with orbital angular momentum) to 180° (spin antialigned); $a_i = |c\mathbf{S}_i/Gm_i^2|$ is the (dimensionless) spin magnitude, which ranges from 0 to 1, and $i = 1$ for the primary black hole and $i = 2$ for the secondary. We use the Newtonian angular momentum for \mathbf{L} , such that it is normal to the orbital plane; the total orbital angular momentum differs from this because of post-Newtonian corrections. We infer that $\chi_{\text{eff}} = -0.12^{+0.21}_{-0.30}$. Similarly to GW150914 [5,37,44], χ_{eff} is close to zero with a preference towards being negative: the probability that $\chi_{\text{eff}} < 0$ is 0.82. Our measurements therefore disfavor a large total spin positively aligned with the orbital angular momentum, but do not exclude zero spins.

The in-plane components of the spin control the amount of precession of the orbit [62]. This may be quantified by the effective precession spin parameter χ_p which ranges from 0 (no precession) to 1 (maximal precession) [39]. Figure 3 (top) shows the posterior probability density for χ_{eff} and χ_p [39]. We gain some information on χ_{eff} , excluding large positive values, but, as for previous events [3,5,37], the χ_p posterior is dominated by the prior (see Sec. III of the Supplemental Material [11]). No meaningful constraints can be placed on the magnitudes of the in-plane spin components and hence precession.

The inferred component spin magnitudes and orientations are shown in Fig. 3 (bottom). The lack of constraints on the in-plane spin components means that we learn almost nothing about the spin magnitudes. The secondary's spin is less well constrained as the less massive component has a smaller impact on the signal. The probability that the tilt θ_{LS_i} is less than 45° is 0.04 for the primary black hole and 0.08 for the secondary, whereas the prior probability is 0.15 for each. Considering the two spins together, the probability that both tilt angles are less than 90° is 0.05.

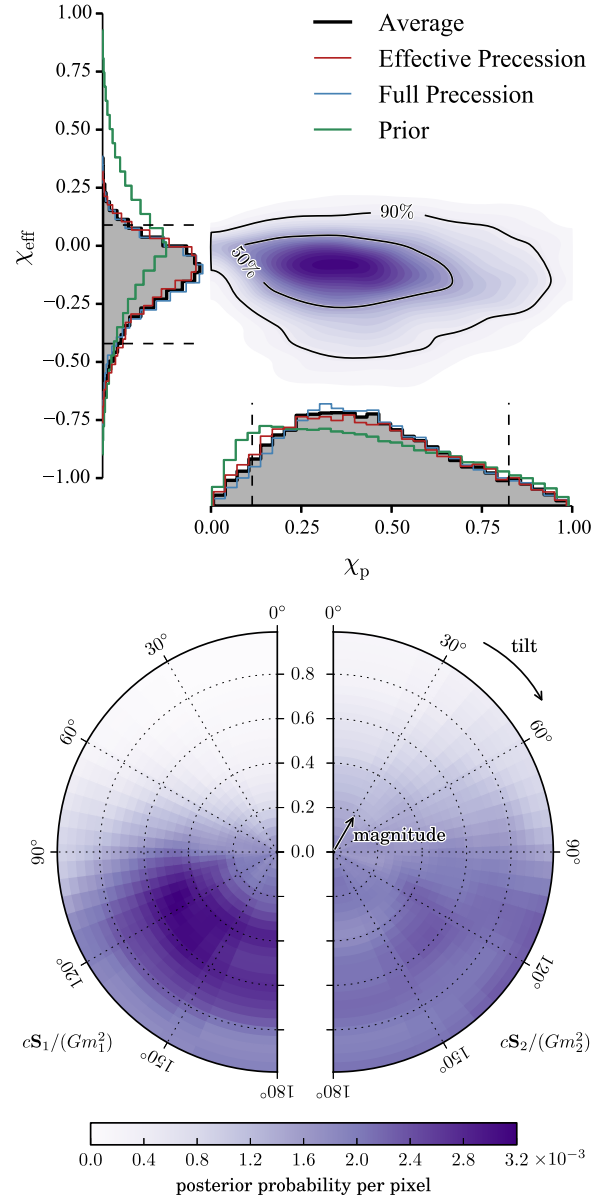


FIG. 3. *Top:* Posterior probability density for the effective inspiral and precession spin parameters, χ_{eff} and χ_p . The one-dimensional distributions show the posteriors for the two waveform models, their average (black), and the prior distributions (green). The dashed lines mark the 90% credible interval for the average posterior. The two-dimensional plot shows the 50% and 90% credible regions plotted over the posterior density function. *Bottom:* Posterior probabilities for the dimensionless component spins, $c\mathbf{S}_1/(Gm_1^2)$ and $c\mathbf{S}_2/(Gm_2^2)$, relative to the normal of the orbital plane $\hat{\mathbf{L}}$. The tilt angles are 0° for spins aligned with the orbital angular momentum and 180° for spins antialigned. The probabilities are marginalized over the azimuthal angles. The pixels have equal prior probability (1.6×10^{-3}); they are spaced linearly in spin magnitudes and the cosine of the tilt angles. Results are given at a gravitational-wave frequency of 20 Hz.

Effectively all of the information comes from constraints on χ_{eff} combined with the mass ratio (and our prior of isotropically distributed orientations and uniformly distributed magnitudes) [5].

The source's luminosity distance D_L is inferred from the signal amplitude [37,74]. The amplitude is inversely proportional to the distance, but also depends upon the binary's inclination [59,75–77]. This degeneracy is a significant source of uncertainty [57,71]. The inclination has a bimodal distribution with broad peaks for face-on and face-off orientations (see Fig. 4 of the Supplemental Material [11]). GW170104's source is at $D_L = 880^{+450}_{-390}$ Mpc, corresponding to a cosmological redshift of $z = 0.18^{+0.08}_{-0.07}$ [52]. While GW170104's source has masses and spins comparable to GW150914's, it is most probably at a greater distance [5,37].

For GW150914, extensive studies were made to verify the accuracy of the model waveforms for parameter estimation through comparisons with numerical-relativity waveforms [78,79]. GW170104 is a similar system to GW150914 and, therefore, it is unlikely that there are any significant biases in our results as a consequence of waveform modeling. The lower SNR of GW170104 makes additional effects not incorporated in the waveform models, such as higher modes [55,80,81], less important. However, if the source is edge on or strongly precessing, there could be significant biases in quantities including \mathcal{M} and χ_{eff} [78]. Comparison to numerical-relativity simulations of binary black holes with nonprecessing spins [79], including those designed to replicate GW170104, produced results (and residuals) consistent with the model-waveform analysis.

V. WAVEFORM RECONSTRUCTIONS

Consistency of GW170104 with binary black hole waveform models can also be explored through comparisons with a morphology-independent signal model [82]. We choose to describe the signal as a superposition of an arbitrary number of Morlet-Gabor wavelets, which models an elliptically polarized, coherent signal in the detector network. Figure 4 plots whitened detector data at the time of GW170104, together with waveforms drawn from the 90% credible region of the posterior distributions of the morphology-independent model and the binary black hole waveform models used to infer the source properties. The signal appears in the two detectors with slightly different amplitudes, and a relative phase shift of approximately 180° , because of their different spatial orientations [2]. The wavelet- and template-based reconstructions differ at early times because the wavelet basis requires high-amplitude, well-localized signal energy to justify the presence of additional wavelets, while the earlier portion of the signal is inherently included in the binary black hole waveform model.

The waveforms reconstructed from the morphology-independent model are consistent with the characteristic inspiral-merger-ringdown structure. The overlap [58]

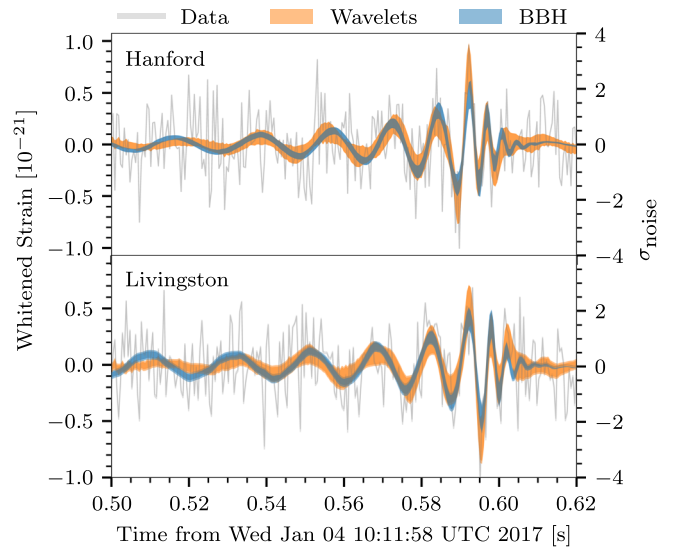


FIG. 4. Time-domain detector data (gray), and 90% confidence intervals for waveforms reconstructed from the morphology-independent wavelet analysis (orange) and binary black hole (BBH) models from both waveform families (blue), whitened by each instrument's noise amplitude spectral density. The left ordinate axes are normalized such that the amplitude of the whitened data and the physical strain are equal at 200 Hz. The right ordinate axes are in units of noise standard deviations. The width of the BBH region is dominated by the uncertainty in the astrophysical parameters.

between the maximum-likelihood waveform of the binary black hole model and the median waveform of the morphology-independent analysis is 87%, consistent with expectations from Monte Carlo analysis of binary black hole signals injected into detector data [34]. We also use the morphology-independent analysis to search for residual gravitational-wave energy after subtracting the maximum-likelihood binary black hole signal from the measured strain data. There is an 83% posterior probability in favor of Gaussian noise versus residual coherent gravitational-wave energy which is not described by the waveform model, implying that GW170104's source is a black hole binary.

VI. BINARY BLACK HOLE POPULATIONS AND MERGER RATES

The addition of the first 11 days of coincident observing time in the second observing run, and the detection of GW170104, leads to an improved estimate of the rate density of binary black hole mergers. We adopt two simple representative astrophysical population models: a distribution that is a power law in m_1 and uniform in m_2 , $p(m_1, m_2) \propto m_1^{-\alpha}/(m_1 - 5M_\odot)$ with $\alpha = 2.35$ [83], and a distribution uniform in the logarithm of each of the component masses [5,8]. In both cases, we impose $m_1, m_2 \geq 5M_\odot$ and $M \leq 100M_\odot$ [8]. Using the results from the first observing run as a prior, we obtain updated rates estimates of $R = 103^{+110}_{-63} \text{ Gpc}^{-3} \text{ yr}^{-1}$ for the power

law, and $R = 32^{+33}_{-20} \text{ Gpc}^{-3} \text{ yr}^{-1}$ for the uniform-in-log distribution [5]. These combine search results from the two offline matched filter analyses, and marginalize over the calibration uncertainty [32]. The range for the merger rate that brackets the two distributions, $12\text{--}213 \text{ Gpc}^{-3} \text{ yr}^{-1}$, is consistent with the range $9\text{--}240 \text{ Gpc}^{-3} \text{ yr}^{-1}$ estimated from the first observing run [5,8]. Recalculating the rates directly after observing a new event can bias rate estimates, but this bias decreases with increasing event count and is negligible compared to other uncertainties on the intervals. While the median estimates have not changed appreciably, the overall tightening in the credible intervals is consistent with the additional observation time and the increment in the number of events with significant probability of being astrophysical from 3 to 4.

Following the first observing run, we performed a hierarchical analysis using the inferred masses of GW150914, LVT151012, and GW151226 to constrain the binary black hole mass distribution. We assumed the power-law population distribution described above, treating α as a parameter to be estimated, and found $\alpha = 2.5^{+1.5}_{-1.6}$ [5]. With the addition of GW170104, α is estimated to be $2.3^{+1.3}_{-1.4}$ (see Sec. IV of the Supplemental Material [11]); the median is close to the power-law exponent used to infer the (higher) merger rates.

VII. ASTROPHYSICAL IMPLICATIONS

GW170104's source is a heavy stellar-mass binary black hole system. Such binaries are consistent with formation through several different evolutionary pathways [6]. Assuming black holes of stellar origin, there are two broad families of formation channels: dynamical and isolated binary evolution. Dynamical assembly of binaries is expected in dense stellar clusters [84–91]. Dynamical influences are also important for binary coalescences near galactic nuclei [92–94], and through interactions as part of a triple [95,96]. Isolated binary evolution in galactic fields classically proceeds via a common envelope [97–105]. Variants avoiding common-envelope evolution include (quasi-)chemically homogeneous evolution of massive tidally locked binaries [101,106,107], or through stable mass transfer in Population I [108,109] or Population III binaries [110,111].

Stars lose mass throughout their lives; to leave a heavy black hole as a remnant they must avoid significant mass loss. Low-metallicity progenitors are believed to have weaker stellar winds and hence diminished mass loss [112]. Given the mass of the primary black hole, the progenitors of GW170104 likely formed in a lower metallicity environment $Z \lesssim 0.5Z_{\odot}$ [6,100,113–115], but low mass loss may also have been possible at higher metallicity if the stars were strongly magnetized [116].

An alternative to the stellar-evolution channels would be binaries of primordial black holes [117–120]. GW170104's

component masses lie in a range for which primordial black holes could contribute significantly to the dark matter content of the Universe, but merger rates in such scenarios are uncertain [118,121]. The potential for existing electromagnetic observations to exclude primordial black holes of these masses is an active area of research [119,122–128].

Some of the formation models listed above predict merger rates on the order of $\sim 1\text{--}10 \text{ Gpc}^{-3} \text{ yr}^{-1}$ [85,87,92–96,107,110,115]. Given that the rate intervals have now tightened and the lower bound (from the uniform-in-log distribution) is $\sim 12 \text{ Gpc}^{-3} \text{ yr}^{-1}$, these channels may be insufficient to explain the full rate, but they could contribute to the total rate if there are multiple channels in operation. Future observations will improve the precision of the rate estimation, its redshift dependence, and our knowledge of the mass distribution, making it easier to constrain binary formation channels.

Gravitational-wave observations provide information about the component spins through measurements of χ_{eff} , and these measurements can potentially be used to distinguish different formation channels. Dynamically assembled binaries (of both stellar and primordial black holes) should have an isotropic distribution of spin tilts, with equal probability for positive and negative χ_{eff} , and a concentration around zero [129]. Isolated binary evolution typically predicts moderate ($\lesssim 45^\circ$) spin misalignments [130], since the effect of many astrophysical processes, such as mass transfer [131,132] and tides [133,134], is to align spins with the orbital angular momentum. Black hole spins could become misaligned due to supernova explosions or torques during collapse. Large natal kicks are needed to produce negative χ_{eff} by changing the orbital plane [129,130,135]. The magnitude of these kicks is currently uncertain [136–141] and also influences the merger rate, with high kicks producing lower merger rates in some population-synthesis models [98,100,115,142]. For binary neutron stars there is evidence that large tilts may be possible with small kicks [143–146], and it is not yet understood if similar torques could occur for black holes [138,147–149]. The absolute value of χ_{eff} depends on the spin magnitudes. Small values of $|\chi_{\text{eff}}|$ can arise because the spin magnitudes are low, or because they are misaligned with the orbital angular momentum or each other. The spin magnitudes for binary black holes are currently uncertain, but GW151226 demonstrated that they can be $\gtrsim 0.2$ [3], and high-mass x-ray binary measurements indicate that the distribution of black hole spins could extend to larger magnitudes [147]. For GW170104, we infer $\chi_{\text{eff}} = -0.12^{+0.21}_{-0.30}$. This includes the possibility of negative χ_{eff} , which would indicate spin-orbit misalignment of at least one component. It also excludes large positive values, and thus could argue against its source forming through chemically homogeneous evolution, since large aligned spins ($a_i \gtrsim 0.4$) would be expected assuming the complete collapse of the progenitor stars [106]. The inferred range is consistent with dynamical assembly and isolated binary

evolution provided that the positive orbit-aligned spin is small (whether due to low spins or misalignment) [129,150–152]. Current gravitational-wave measurements cluster around $\chi_{\text{eff}} \sim 0$ ($|\chi_{\text{eff}}| < 0.35$ at the 90% credible level for all events; see Fig. 5 of the Supplemental Material [11]) [5]. Assuming that binary black hole spins are not typically small ($\lesssim 0.2$), our observations hint towards the astrophysical population favoring a distribution of misaligned spins rather than near orbit-aligned spins [153]; further detections will test if this is the case, and enable us to distinguish different spin magnitude and orientation distributions [154–159].

VIII. TESTS OF GENERAL RELATIVITY

To check the consistency of the observed signals with the predictions of GR for binary black holes in quasicircular orbit, we employ a phenomenological approach that probes how gravitational-wave generation or propagation could be modified in an alternative theory of gravity. Testing for these characteristic modifications in the waveform can quantify the degree to which departures from GR can be tolerated given the data. First, we consider the possibility of a modified gravitational-wave dispersion relation, and place bounds on the magnitude of potential deviations from GR. Second, we perform null tests to quantify generic deviations from GR: without assuming a specific alternative theory of gravity, we verify if the detected signal is compatible with GR. For these tests we use the three confident detections (GW150914, GW151226, and GW170104); we do not use the marginal event LVT151012, as its low SNR means that it contributes insignificantly to all the tests [5].

A. Modified dispersion

In GR, gravitational waves are nondispersive. We consider a modified dispersion relation of the form $E^2 = p^2 c^2 + A p^\alpha c^\alpha$, $\alpha \geq 0$, that leads to dephasing of the waves relative to the phase evolution in GR. Here E and p are the energy and momentum of gravitational radiation, and A is the amplitude of the dispersion [160,161]. Modifications to the dispersion relation can arise in theories that include violations of local Lorentz invariance [162]. Lorentz invariance is a cornerstone of modern physics but its violation is expected in certain quantum gravity frameworks [162,163]. Several modified theories of gravity predict specific values of α , including massive-graviton theories ($\alpha = 0$, $A > 0$) [163], multifractal spacetime [164] ($\alpha = 2.5$), doubly special relativity [165] ($\alpha = 3$), and Hořava-Lifshitz [166] and extra-dimensional [167] theories ($\alpha = 4$). For our analysis, we assume that the only effect of these alternative theories is to modify the dispersion relation.

To leading order in $A E^{\alpha-2}$, the group velocity of gravitational waves is modified as $v_g/c = 1 + (\alpha - 1) A E^{\alpha-2}/2$ [161]; both superluminal and subluminal propagation velocities are possible, depending on the sign of A and the value of α . A change in the dispersion relation leads to an extra term

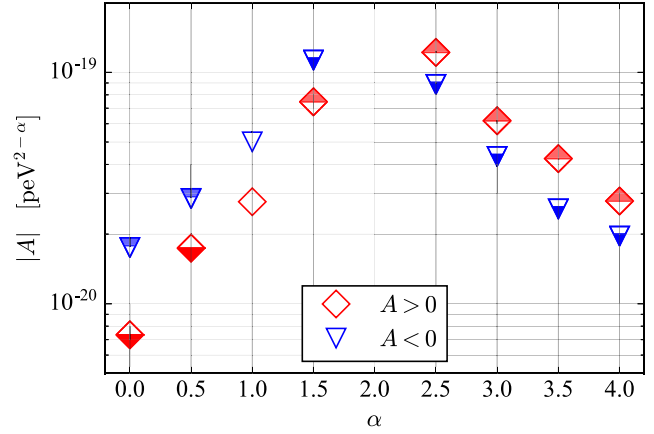


FIG. 5. 90% credible upper bounds on $|A|$, the magnitude of dispersion, obtained combining the posteriors of GW170104 with those of GW150914 and GW151226. We use picoelectronvolts as a convenient unit because the corresponding frequency scale is around where GW170104 has greatest amplitude ($1 \text{ peV} \approx h \times 250 \text{ Hz}$, where h is the Planck constant). General relativity corresponds to $A = 0$. Markers filled at the top (bottom) correspond to values of $|A|$ and α for which gravitational waves travel with superluminal (subluminal) speed.

$\delta\Psi(A, \alpha)$ in the evolution of the gravitational-wave phase [160]. We introduce such a term in the effective-precession waveform model [38] to constrain dispersion for various values of α . To this end, we assume flat priors on A . In Fig. 5 we show 90% credible upper bounds on $|A|$ derived from the three confident detections. We do not show results for $\alpha = 2$ since in this case the modification of the gravitational-wave phase is degenerate with the arrival time of the signal.

There exist constraints on Lorentz invariance violating dispersion relations from other observational sectors (e.g., photon or neutrino observations) for certain values of α , and our results are weaker by several orders of magnitude. However, there are frameworks in which Lorentz invariance is only broken in one sector [168,169], implying that each sector provides complementary information on potential modifications to GR. Our results are the first bounds derived from gravitational-wave observations, and the first tests of superluminal propagation in the gravitational sector.

The result for $A > 0$ and $\alpha = 0$ can be reparametrized to derive a lower bound on the graviton Compton wavelength λ_g , assuming that gravitons disperse in vacuum in the same way as massive particles [5,7,170]. In this case, no violation of Lorentz invariance is assumed. Using a flat prior for the graviton mass, we obtain $\lambda_g > 1.5 \times 10^{13} \text{ km}$, which improves on the bound of $1.0 \times 10^{13} \text{ km}$ from previous gravitational-wave observations [5,7]. The combined bound using the three confident detections is $\lambda_g > 1.6 \times 10^{13} \text{ km}$, or for the graviton mass $m_g \leq 7.7 \times 10^{-23} \text{ eV}/c^2$.

B. Null tests

In the post-Newtonian approximation, the gravitational-wave phase in the Fourier domain is a series expansion in

powers of frequency, the expansion coefficients being functions of the source parameters [60,63,171]. In the effective-precession model, waveforms from numerical-relativity simulations are also modeled using an expansion of the phase in terms of the Fourier frequency. To verify if the detected signal is consistent with GR, we allow the expansion coefficients to deviate in turn from their nominal GR value and we obtain a posterior distribution for the difference between the measured and GR values [172–177]. We find no significant deviation from the predictions of GR [5,7]. Combined bounds for GW170104 and the two confident detections from the first observing run [5] do not significantly improve the bounds on the waveform phase coefficients.

Finally, we investigate whether the merger-ringdown portion of the detected signal is consistent with the inspiral part [7,178,179]. The two parts are divided at 143 Hz, a frequency close to the median inferred (detector-frame) innermost-stable-circular-orbit frequency of the remnant Kerr black hole. For each part, we infer the component masses and spins, and calculate from these the final mass and spin using fits from numerical relativity, as in Sec. IV [45–48]. We then calculate a two-dimensional posterior distribution for the fractional difference between final mass and spin calculated separately from the two parts [7,179]. The expected GR value (no difference in the final mass and spin estimates) lies close to the peak of the posterior distribution, well within the 90% credible region. When combined with the posteriors from GW150914, the width of the credible intervals decreases by a factor of ~ 1.5 , providing a better constraint on potential deviations from GR.

In conclusion, in agreement with the predictions of GR, none of the tests we performed indicate a statistically significant departure from the coalescence of Kerr black holes in a quasicircular orbit.

IX. CONCLUSIONS

Advanced LIGO began its second observing run on November 30, 2016, and on January 4, 2017 the LIGO-Hanford and LIGO-Livingston detectors registered a highly significant gravitational-wave signal GW170104 from the coalescence of two stellar-mass black holes. GW170104 joins two other high-significance events [2,3] and a marginal candidate [4] from Advanced LIGO’s first observing run [5]. This new detection is entirely consistent with the astrophysical rates inferred from the previous run. The source is a heavy binary black hole system, similar to that of GW150914. Spin configurations with both component spins aligned with the orbital angular momentum are disfavored (but not excluded); we do not significantly constrain the component black holes’ spin magnitudes. The observing run will continue until mid 2017. Expanding the catalog of binary black holes will provide further insight into their formation and evolution, and allow for tighter constraints on potential modifications to GR.

Further details of the analysis and the results are given in the Supplemental Material [11]. Data for this event are available at the LIGO Open Science Center [180].

ACKNOWLEDGMENTS

The authors gratefully acknowledge the support of the United States National Science Foundation (NSF) for the construction and operation of the LIGO Laboratory and Advanced LIGO as well as the Science and Technology Facilities Council (STFC) of the United Kingdom, the Max-Planck-Society (MPS), and the State of Niedersachsen/Germany for support of the construction of Advanced LIGO and construction and operation of the GEO 600 detector. Additional support for Advanced LIGO was provided by the Australian Research Council. The authors gratefully acknowledge the Italian Istituto Nazionale di Fisica Nucleare (INFN), the French Centre National de la Recherche Scientifique (CNRS) and the Foundation for Fundamental Research on Matter supported by the Netherlands Organisation for Scientific Research, for the construction and operation of the Virgo detector and the creation and support of the EGO consortium. The authors also gratefully acknowledge research support from these agencies as well as by the Council of Scientific and Industrial Research of India, Department of Science and Technology, India, Science & Engineering Research Board (SERB), India, Ministry of Human Resource Development, India, the Spanish Ministerio de Economía y Competitividad, the Vicepresidència i Conselleria d’Innovació, Recerca i Turisme and the Conselleria d’Educació i Universitat del Govern de les Illes Balears, the National Science Centre of Poland, the European Commission, the Royal Society, the Scottish Funding Council, the Scottish Universities Physics Alliance, the Hungarian Scientific Research Fund (OTKA), the Lyon Institute of Origins (LIO), the National Research Foundation of Korea, Industry Canada and the Province of Ontario through the Ministry of Economic Development and Innovation, the Natural Science and Engineering Research Council Canada, Canadian Institute for Advanced Research, the Brazilian Ministry of Science, Technology, and Innovation, International Center for Theoretical Physics South American Institute for Fundamental Research (ICTP-SAIFR), Russian Foundation for Basic Research, the Leverhulme Trust, the Research Corporation, Ministry of Science and Technology (MOST), Taiwan, and the Kavli Foundation. The authors gratefully acknowledge the support of the NSF, STFC, MPS, INFN, CNRS, and the State of Niedersachsen/Germany for provision of computational resources. This article has been assigned the document number LIGO-P170104.

[1] J. Aasi *et al.* (LIGO Scientific Collaboration), *Classical Quantum Gravity* **32**, 074001 (2015).

- [2] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 061102 (2016).
- [3] B. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 241103 (2016).
- [4] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. D* **93**, 122003 (2016).
- [5] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. X* **6**, 041015 (2016).
- [6] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Astrophys. J. Lett.* **818**, L22 (2016).
- [7] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 221101 (2016).
- [8] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Astrophys. J. Lett.* **833**, L1 (2016).
- [9] S. Chatterji, L. Blackburn, G. Martin, and E. Katsavounidis, *Classical Quantum Gravity* **21**, S1809 (2004).
- [10] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 131103 (2016).
- [11] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.118.221101> for technical details and additional results.
- [12] S. Karki *et al.*, *Rev. Sci. Instrum.* **87**, 114503 (2016).
- [13] B. P. Abbott *et al.* (LIGO Scientific Collaboration), *Phys. Rev. D* **95**, 062003 (2017).
- [14] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Classical Quantum Gravity* **33**, 134001 (2016).
- [15] T. Dal Canton *et al.*, *Phys. Rev. D* **90**, 082004 (2014).
- [16] S. A. Usman *et al.*, *Classical Quantum Gravity* **33**, 215004 (2016).
- [17] A. H. Nitz, I. W. Harry, J. L. Willis, C. M. Biwer, D. A. Brown, L. P. Pekowsky, T. Dal Canton, A. R. Williamson, T. Dent, C. D. Capano, T. J. Massinger, A. K. Lenon, A. B. Nielsen, and M. Cabero, PyCBC Software, <https://github.com/ligo-cbc/pycbc> (2017).
- [18] L. P. Singer and L. R. Price, *Phys. Rev. D* **93**, 024013 (2016).
- [19] L. P. Singer *et al.*, *Astrophys. J. Lett.* **829**, L15 (2016).
- [20] LIGO Scientific Collaboration and Virgo Collaboration, Gamma-ray Coordinates Network/Transient Astronomy Network Circular 20364 (2017) [<https://gcn.gsfc.nasa.gov/gcn3/20364.gcn3>].
- [21] The collection of Circulars exchanged with collaborating astronomers regarding this event is archived at <https://gcn.gsfc.nasa.gov/other/G268556.gcn3>.
- [22] C. Messick *et al.*, *Phys. Rev. D* **95**, 042001 (2017).
- [23] C. Capano, I. Harry, S. Privitera, and A. Buonanno, *Phys. Rev. D* **93**, 124007 (2016).
- [24] D. A. Brown, I. Harry, A. Lundgren, and A. H. Nitz, *Phys. Rev. D* **86**, 084017 (2012).
- [25] I. W. Harry, B. Allen, and B. S. Sathyaprakash, *Phys. Rev. D* **80**, 104014 (2009).
- [26] P. Ajith, N. Fotopoulos, S. Privitera, A. Neunzert, N. Mazumder, and A. J. Weinstein, *Phys. Rev. D* **89**, 084041 (2014).
- [27] B. S. Sathyaprakash and S. V. Dhurandhar, *Phys. Rev. D* **44**, 3819 (1991).
- [28] B. J. Owen and B. S. Sathyaprakash, *Phys. Rev. D* **60**, 022002 (1999).
- [29] A. Bohé *et al.*, *Phys. Rev. D* **95**, 044028 (2017).
- [30] T. Dal Canton and I. Harry, [arXiv:1705.01845](https://arxiv.org/abs/1705.01845).
- [31] A. H. Nitz, T. Dent, T. Dal Canton, S. Fairhurst, and D. Brown, [arXiv:1705.01513](https://arxiv.org/abs/1705.01513).
- [32] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Astrophys. J. Suppl. Ser.* **227**, 14 (2016).
- [33] W. M. Farr, J. R. Gair, I. Mandel, and C. Cutler, *Phys. Rev. D* **91**, 023005 (2015).
- [34] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. D* **93**, 122004 (2016); **94**, 069903 (2016) (Addendum).
- [35] S. Klimenko *et al.*, *Phys. Rev. D* **93**, 042004 (2016).
- [36] J. Veitch *et al.*, *Phys. Rev. D* **91**, 042003 (2015).
- [37] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. Lett.* **116**, 241102 (2016).
- [38] M. Hannam, P. Schmidt, A. Bohé, L. Haegel, S. Husa, F. Ohme, G. Pratten, and M. Pürrer, *Phys. Rev. Lett.* **113**, 151101 (2014).
- [39] P. Schmidt, F. Ohme, and M. Hannam, *Phys. Rev. D* **91**, 024043 (2015).
- [40] S. Khan, S. Husa, M. Hannam, F. Ohme, M. Pürrer, X. Jiménez Forteza, and A. Bohé, *Phys. Rev. D* **93**, 044007 (2016).
- [41] Y. Pan, A. Buonanno, A. Taracchini, L. E. Kidder, A. H. Mroué, H. P. Pfeiffer, M. A. Scheel, and B. Szilágyi, *Phys. Rev. D* **89**, 084006 (2014).
- [42] A. Taracchini *et al.*, *Phys. Rev. D* **89**, 061502 (2014).
- [43] S. Babak, A. Taracchini, and A. Buonanno, *Phys. Rev. D* **95**, 024010 (2017).
- [44] B. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. X* **6**, 041014 (2016).
- [45] F. Hofmann, E. Barausse, and L. Rezzolla, *Astrophys. J. Lett.* **825**, L19 (2016).
- [46] X. Jiménez-Forteza, D. Keitel, S. Husa, M. Hannam, S. Khan, and M. Pürrer, *Phys. Rev. D* **95**, 064024 (2017).
- [47] J. Healy and C. O. Lousto, *Phys. Rev. D* **95**, 024037 (2017).
- [48] N. K. Johnson-McDaniel *et al.*, LIGO Scientific Collaboration and Virgo Collaboration Technical Report No. LIGO-T1600168, 2016 [<https://dcc.ligo.org/LIGO-T1600168/public>].
- [49] D. Keitel *et al.*, [arXiv:1612.09566](https://arxiv.org/abs/1612.09566).
- [50] A. Krolak and B. F. Schutz, *Gen. Relativ. Gravit.* **19**, 1163 (1987).
- [51] D. E. Holz and S. A. Hughes, *Astrophys. J.* **629**, 15 (2005).
- [52] P. A. R. Ade *et al.* (Planck Collaboration), *Astron. Astrophys.* **594**, A13 (2016).
- [53] P. Ajith and S. Bose, *Phys. Rev. D* **79**, 084032 (2009).
- [54] J. Veitch, M. Pürrer, and I. Mandel, *Phys. Rev. Lett.* **115**, 141101 (2015).
- [55] P. B. Graff, A. Buonanno, and B. S. Sathyaprakash, *Phys. Rev. D* **92**, 022002 (2015).
- [56] C.-J. Haster, Z. Wang, C. P. L. Berry, S. Stevenson, J. Veitch, and I. Mandel, *Mon. Not. R. Astron. Soc.* **457**, 4499 (2016).
- [57] A. Ghosh, W. Del Pozzo, and P. Ajith, *Phys. Rev. D* **94**, 104070 (2016).
- [58] L. S. Finn and D. F. Chernoff, *Phys. Rev. D* **47**, 2198 (1993).

- [59] C. Cutler and É. E. Flanagan, *Phys. Rev. D* **49**, 2658 (1994).
- [60] L. Blanchet, T. Damour, B. R. Iyer, C. M. Will, and A. G. Wiseman, *Phys. Rev. Lett.* **74**, 3515 (1995).
- [61] S. Vitale, R. Lynch, J. Veitch, V. Raymond, and R. Sturani, *Phys. Rev. Lett.* **112**, 251101 (2014).
- [62] T. A. Apostolatos, C. Cutler, G. J. Sussman, and K. S. Thorne, *Phys. Rev. D* **49**, 6274 (1994).
- [63] L. Blanchet, *Living Rev. Relativ.* **17**, 2 (2014) [arXiv:1310.1528].
- [64] T. Damour, *Phys. Rev. D* **64**, 124013 (2001).
- [65] P. Ajith *et al.*, *Phys. Rev. Lett.* **106**, 241101 (2011).
- [66] L. Santamaría *et al.*, *Phys. Rev. D* **82**, 064016 (2010).
- [67] M. Campanelli, C. O. Lousto, and Y. Zlochower, *Phys. Rev. D* **74**, 041501 (2006).
- [68] C. Reisswig, S. Husa, L. Rezzolla, E. N. Dorband, D. Pollney, and J. Seiler, *Phys. Rev. D* **80**, 124026 (2009).
- [69] M. Pürrer, M. Hannam, P. Ajith, and S. Husa, *Phys. Rev. D* **88**, 064007 (2013).
- [70] M. Pürrer, M. Hannam, and F. Ohme, *Phys. Rev. D* **93**, 084042 (2016).
- [71] S. Vitale, R. Lynch, V. Raymond, R. Sturani, J. Veitch, and P. Graff, *Phys. Rev. D* **95**, 064053 (2017).
- [72] É. Racine, *Phys. Rev. D* **78**, 044021 (2008).
- [73] D. Gerosa, M. Kesden, U. Sperhake, E. Berti, and R. O’Shaughnessy, *Phys. Rev. D* **92**, 064016 (2015).
- [74] B. F. Schutz, *Nature (London)* **323**, 310 (1986).
- [75] S. Nissanke, D. E. Holz, S. A. Hughes, N. Dalal, and J. L. Sievers, *Astrophys. J.* **725**, 496 (2010).
- [76] C. L. Rodriguez, B. Farr, V. Raymond, W. M. Farr, T. B. Littenberg, D. Fazi, and V. Kalogera, *Astrophys. J.* **784**, 119 (2014).
- [77] B. Farr *et al.*, *Astrophys. J.* **825**, 116 (2016).
- [78] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Classical Quantum Gravity* **34**, 104002 (2017).
- [79] B. P. Abbott *et al.* (LIGO Scientific Collaboration and Virgo Collaboration), *Phys. Rev. D* **94**, 064035 (2016).
- [80] V. Varma, P. Ajith, S. Husa, J. C. Bustillo, M. Hannam, and M. Pürrer, *Phys. Rev. D* **90**, 124004 (2014).
- [81] J. Calderón Bustillo, S. Husa, A. M. Sintes, and M. Pürrer, *Phys. Rev. D* **93**, 084019 (2016).
- [82] N. J. Cornish and T. B. Littenberg, *Classical Quantum Gravity* **32**, 135012 (2015).
- [83] E. E. Salpeter, *Astrophys. J.* **121**, 161 (1955).
- [84] S. F. Portegies Zwart and S. McMillan, *Astrophys. J. Lett.* **528**, L17 (2000).
- [85] C. L. Rodriguez, C.-J. Haster, S. Chatterjee, V. Kalogera, and F. A. Rasio, *Astrophys. J. Lett.* **824**, L8 (2016).
- [86] R. M. O’Leary, Y. Meiron, and B. Kocsis, *Astrophys. J. Lett.* **824**, L12 (2016).
- [87] M. Mapelli, *Mon. Not. R. Astron. Soc.* **459**, 3432 (2016).
- [88] S. Banerjee, *Mon. Not. R. Astron. Soc.* **467**, 524 (2017).
- [89] J. R. Hurley, A. C. Sippel, C. A. Tout, and S. J. Aarseth, *Pub. Astron. Soc. Aust.* **33**, e036 (2016).
- [90] A. Askar, M. Szkudlarek, D. Gondek-Rosińska, M. Giersz, and T. Bulik, *Mon. Not. R. Astron. Soc. Lett.* **464**, L36 (2017).
- [91] D. Park, C. Kim, H. M. Lee, Y.-B. Bae, and C. Belczynski, arXiv:1703.01568 [Mon. Not. R. Astron. Soc. (in press)].
- [92] N. C. Stone, B. D. Metzger, and Z. Haiman, *Mon. Not. R. Astron. Soc.* **464**, 946 (2017).
- [93] I. Bartos, B. Kocsis, Z. Haiman, and S. Márka, *Astrophys. J.* **835**, 165 (2017).
- [94] F. Antonini and F. A. Rasio, *Astrophys. J.* **831**, 187 (2016).
- [95] K. Silsbee and S. Tremaine, *Astrophys. J.* **836**, 39 (2017).
- [96] F. Antonini, S. Toonen, and A. S. Hamers, arXiv:1703.06614 [Astrophys. J. (to be published)].
- [97] A. Tutukov and L. Yungelson, *Nauchnye Informatsii* **27**, 70 (1973) [http://adsabs.harvard.edu/abs/1973NInfo..27..70T].
- [98] R. Voss and T. M. Tauris, *Mon. Not. R. Astron. Soc.* **342**, 1169 (2003).
- [99] N. Mennekens and D. Vanbeveren, *Astron. Astrophys.* **564**, A134 (2014).
- [100] K. Belczynski, D. E. Holz, T. Bulik, and R. O’Shaughnessy, *Nature (London)* **534**, 512 (2016).
- [101] J. J. Eldridge and E. R. Stanway, *Mon. Not. R. Astron. Soc.* **462**, 3302 (2016).
- [102] V. M. Lipunov, V. Kornilov, E. Gorbovskoy, N. Tiurina, P. Balanutsa, and A. Kuznetsov, *New Astron.* **51**, 122 (2017).
- [103] S. E. Woosley, *Astrophys. J. Lett.* **824**, L10 (2016).
- [104] M. U. Kruckow, T. M. Tauris, N. Langer, D. Szécsi, P. Marchant, and P. Podsiadlowski, *Astron. Astrophys.* **596**, A58 (2016).
- [105] S. Stevenson, A. Vigna-Gómez, I. Mandel, J. W. Barrett, C. J. Neijssel, D. Perkins, and S. E. de Mink, *Nat. Commun.* **8**, 14906 (2017).
- [106] P. Marchant, N. Langer, P. Podsiadlowski, T. M. Tauris, and T. J. Moriya, *Astron. Astrophys.* **588**, A50 (2016).
- [107] I. Mandel and S. E. de Mink, *Mon. Not. R. Astron. Soc.* **458**, 2634 (2016).
- [108] K. Pavlovskii, N. Ivanova, K. Belczynski, and K. X. Van, *Mon. Not. R. Astron. Soc.* **465**, 2092 (2017).
- [109] E. P. J. van den Heuvel, S. F. Portegies Zwart, and S. E. de Mink, arXiv:1701.02355.
- [110] T. Hartwig, M. Volonteri, V. Bromm, R. S. Klessen, E. Barausse, M. Magg, and A. Stacy, *Mon. Not. R. Astron. Soc. Lett.* **460**, L74 (2016).
- [111] K. Inayoshi, R. Hirai, T. Kinugawa, and K. Hotokezaka, arXiv:1701.04823 [Mon. Not. R. Astron. Soc. (to be published)].
- [112] J. S. Vink, *New Astron. Rev.* **52**, 419 (2008).
- [113] K. Belczynski, T. Bulik, C. L. Fryer, A. Ruiter, J. S. Vink, and J. R. Hurley, *Astrophys. J.* **714**, 1217 (2010).
- [114] M. Spera, M. Mapelli, and A. Bressan, *Mon. Not. R. Astron. Soc.* **451**, 4086 (2015).
- [115] C. L. Rodriguez, S. Chatterjee, and F. A. Rasio, *Phys. Rev. D* **93**, 084029 (2016).
- [116] V. Petit, Z. Keszthelyi, R. MacInnis, D. H. Cohen, R. H. D. Townsend, G. A. Wade, S. L. Thomas, S. P. Owocki, J. Puls, and J. A. ud-Doula, *Mon. Not. R. Astron. Soc.* **466**, 1052 (2017).
- [117] B. J. Carr and S. W. Hawking, *Mon. Not. R. Astron. Soc.* **168**, 399 (1974).
- [118] S. Bird, I. Cholis, J. B. Muñoz, Y. Ali-Haïmoud, M. Kamionkowski, E. D. Kovetz, A. Raccanelli, and A. G. Riess, *Phys. Rev. Lett.* **116**, 201301 (2016).
- [119] S. Clesse and J. García-Bellido, *Phys. Dark Universe* **15**, 142 (2017).

- [120] B. Carr, F. Kühnel, and M. Sandstad, *Phys. Rev. D* **94**, 083504 (2016).
- [121] M. Sasaki, T. Suyama, T. Tanaka, and S. Yokoyama, *Phys. Rev. Lett.* **117**, 061101 (2016).
- [122] M. Ricotti, J. P. Ostriker, and K. J. Mack, *Astrophys. J.* **680**, 829 (2008).
- [123] S. Clesse and J. García-Bellido, *Phys. Rev. D* **92**, 023524 (2015).
- [124] A. Kashlinsky, *Astrophys. J. Lett.* **823**, L25 (2016).
- [125] A. M. Green, *Phys. Rev. D* **94**, 063530 (2016).
- [126] Y. Ali-Haïmoud and M. Kamionkowski, *Phys. Rev. D* **95**, 043534 (2017).
- [127] E. Mediavilla, J. Jiménez-Vicente, J. A. Muñoz, H. Vives-Arias, and J. Calderón-Infante, *Astrophys. J. Lett.* **836**, L18 (2017).
- [128] B. Carr, M. Raidal, T. Tenkanen, V. Vaskonen, and H. Veermäe, [arXiv:1705.05567](https://arxiv.org/abs/1705.05567).
- [129] C. L. Rodriguez, M. Zevin, C. Pankow, V. Kalogera, and F. A. Rasio, *Astrophys. J. Lett.* **832**, L2 (2016).
- [130] V. Kalogera, *Astrophys. J.* **541**, 319 (2000).
- [131] J. M. Bardeen and J. A. Petterson, *Astrophys. J. Suppl. Ser.* **195**, L65 (1975).
- [132] A. R. King, S. H. Lubow, G. I. Ogilvie, and J. E. Pringle, *Mon. Not. R. Astron. Soc.* **363**, 49 (2005).
- [133] J. P. Zahn, *Astron. Astrophys.* **57**, 383 (1977) [<http://adsabs.harvard.edu/abs/1977A%26A....57..383Z>].
- [134] P. Hut, *Astron. Astrophys.* **99**, 126 (1981) [<http://adsabs.harvard.edu/abs/1981A%26A....99..126H>].
- [135] R. O'Shaughnessy, D. Gerosa, and D. Wysocki, [arXiv:1704.03879](https://arxiv.org/abs/1704.03879).
- [136] R. G. Martin, C. A. Tout, and J. E. Pringle, *Mon. Not. R. Astron. Soc.* **401**, 1514 (2010).
- [137] T.-W. Wong, F. Valsecchi, A. Ansari, T. Fragos, E. Glebbeek, V. Kalogera, and J. McClintock, *Astrophys. J.* **790**, 119 (2014).
- [138] H.-T. Janka, *Mon. Not. R. Astron. Soc.* **434**, 1355 (2013).
- [139] S. Repetto and G. Nelemans, *Mon. Not. R. Astron. Soc.* **453**, 3341 (2015).
- [140] I. Mandel, *Mon. Not. R. Astron. Soc.* **456**, 578 (2016).
- [141] S. Repetto, A. P. Igoshev, and G. Nelemans, *Mon. Not. R. Astron. Soc.* **467**, 298 (2017).
- [142] M. Dominik, K. Belczynski, C. Fryer, D. E. Holz, E. Berti, T. Bulik, I. Mandel, and R. O'Shaughnessy, *Astrophys. J.* **779**, 72 (2013).
- [143] H. Spruit and E. S. Phinney, *Nature (London)* **393**, 139 (1998).
- [144] W. M. Farr, K. Kremer, M. Lyutikov, and V. Kalogera, *Astrophys. J.* **742**, 81 (2011).
- [145] R. D. Ferdman *et al.*, *Astrophys. J.* **767**, 85 (2013).
- [146] R. Kazeroni, J. Guilet, and T. Foglizzo, [arXiv:1701.07029](https://arxiv.org/abs/1701.07029).
- [147] M. C. Miller and J. M. Miller, *Phys. Rep.* **548**, 1 (2015).
- [148] T. Fragos and J. E. McClintock, *Astrophys. J.* **800**, 17 (2015).
- [149] J. Fuller, M. Cantiello, D. Lecoanet, and E. Quataert, *Astrophys. J.* **810**, 101 (2015); **815**, 137(E) (2015).
- [150] M. Zaldarriaga, D. Kushnir, and J. A. Kollmeier, [arXiv:1702.00885](https://arxiv.org/abs/1702.00885).
- [151] K. Hotokezaka and T. Piran, [arXiv:1702.03952](https://arxiv.org/abs/1702.03952).
- [152] D. Gerosa, M. Kesden, E. Berti, R. O'Shaughnessy, and U. Sperhake, *Phys. Rev. D* **87**, 104028 (2013).
- [153] W. M. Farr, S. Stevenson, M. C. Miller, A. Vecchio, and I. Mandel, Technical Report No. LIGO-P1700067, 2017 [<https://dcc.ligo.org/P1700067/public>].
- [154] D. Gerosa, R. O'Shaughnessy, M. Kesden, E. Berti, and U. Sperhake, *Phys. Rev. D* **89**, 124025 (2014).
- [155] S. Vitale, R. Lynch, R. Sturani, and P. Graff, *Classical Quantum Gravity* **34**, 03LT01 (2017).
- [156] D. Gerosa and E. Berti, [arXiv:1703.06223](https://arxiv.org/abs/1703.06223).
- [157] M. Fishbach, D. E. Holz, and B. Farr, *Astrophys. J. Lett.* **840**, L24 (2017).
- [158] S. Stevenson, C. P. L. Berry, and I. Mandel, [arXiv:1703.06873](https://arxiv.org/abs/1703.06873).
- [159] C. Talbot and E. Thrane, [arXiv:1704.08370](https://arxiv.org/abs/1704.08370).
- [160] S. Mirshekari, N. Yunes, and C. M. Will, *Phys. Rev. D* **85**, 024041 (2012).
- [161] N. Yunes, K. Yagi, and F. Pretorius, *Phys. Rev. D* **94**, 084002 (2016).
- [162] D. Mattingly, *Living Rev. Relativ.* **8**, 5 (2005) [[arXiv:gr-qc/0502097](https://arxiv.org/abs/gr-qc/0502097)].
- [163] C. M. Will, *Living Rev. Relativ.* **17**, 4 (2014) [[arXiv:1403.7377](https://arxiv.org/abs/1403.7377)].
- [164] G. Calcagni, *Phys. Rev. Lett.* **104**, 251301 (2010).
- [165] G. Amelino-Camelia, *Nature (London)* **418**, 34 (2002).
- [166] P. Hořava, *Phys. Rev. D* **79**, 084008 (2009).
- [167] A. S. Sefiedgar, K. Nozari, and H. R. Sepangi, *Phys. Lett. B* **696**, 119 (2011).
- [168] M. D. Seifert, *Phys. Rev. D* **81**, 065010 (2010).
- [169] B. Altschul, Q. G. Bailey, and V. A. Kostelecky, *Phys. Rev. D* **81**, 065028 (2010).
- [170] C. M. Will, *Phys. Rev. D* **57**, 2061 (1998).
- [171] L. Blanchet, T. Damour, G. Esposito-Farèse, and B. R. Iyer, *Phys. Rev. Lett.* **93**, 091101 (2004).
- [172] L. Blanchet and B. S. Sathyaprakash, *Classical Quantum Gravity* **11**, 2807 (1994).
- [173] L. Blanchet, T. Damour, and B. R. Iyer, *Phys. Rev. D* **51**, 5360 (1995); **54**, 1860(E) (1996).
- [174] K. G. Arun, B. R. Iyer, M. S. S. Qusailah, and B. S. Sathyaprakash, *Phys. Rev. D* **74**, 024006 (2006).
- [175] C. K. Mishra, K. G. Arun, B. R. Iyer, and B. S. Sathyaprakash, *Phys. Rev. D* **82**, 064010 (2010).
- [176] N. Yunes and F. Pretorius, *Phys. Rev. D* **80**, 122003 (2009).
- [177] T. G. F. Li, W. Del Pozzo, S. Vitale, C. Van Den Broeck, M. Agathos, J. Veitch, K. Grover, T. Sidery, R. Sturani, and A. Vecchio, *Phys. Rev. D* **85**, 082003 (2012).
- [178] A. Ghosh *et al.*, *Phys. Rev. D* **94**, 021101 (2016).
- [179] A. Ghosh, N. K. Johnson-McDaniel, A. Ghosh, C. K. Mishra, P. Ajith, W. Del Pozzo, C. P. L. Berry, A. B. Nielsen, and L. London, [arXiv:1704.06784](https://arxiv.org/abs/1704.06784).
- [180] LIGO Scientific Collaboration, LIGO Open Science Center release of GW170104, DOI: [10.7935/K53X84K2](https://doi.org/10.7935/K53X84K2) (2017).

B. P. Abbott,¹ R. Abbott,¹ T. D. Abbott,² F. Acernese,^{3,4} K. Ackley,⁵ C. Adams,⁶ T. Adams,⁷ P. Addesso,⁸ R. X. Adhikari,¹ V. B. Adya,⁹ C. Affeldt,⁹ M. Afrough,¹⁰ B. Agarwal,¹¹ M. Agathos,¹² K. Agatsuma,¹³ N. Aggarwal,¹⁴ O. D. Aguiar,¹⁵ L. Aiello,^{16,17} A. Ain,¹⁸ P. Ajith,¹⁹ B. Allen,^{9,20,21} G. Allen,¹¹ A. Allocca,^{22,23} P. A. Altin,²⁴ A. Amato,²⁵ A. Ananyeva,¹ S. B. Anderson,¹ W. G. Anderson,²⁰ S. Antier,²⁶ S. Appert,¹ K. Arai,¹ M. C. Araya,¹ J. S. Areeda,²⁷ N. Arnaud,^{26,28} K. G. Arun,²⁹ S. Ascenzi,^{30,17} G. Ashton,⁹ M. Ast,³¹ S. M. Aston,⁶ P. Astone,³² P. Aufmuth,²¹ C. Aulbert,⁹ K. AultO'Neal,³³ A. Avila-Alvarez,²⁷ S. Babak,³⁴ P. Bacon,³⁵ M. K. M. Bader,¹³ S. Bae,³⁶ P. T. Baker,^{37,38} F. Baldaccini,^{39,40} G. Ballardini,²⁸ S. W. Ballmer,⁴¹ S. Banagiri,⁴² J. C. Barayoga,¹ S. E. Barclay,⁴³ B. C. Barish,¹ D. Barker,⁴⁴ F. Barone,^{3,4} B. Barr,⁴³ L. Barsotti,¹⁴ M. Barsuglia,³⁵ D. Barta,⁴⁵ J. Bartlett,⁴⁴ I. Bartos,⁴⁶ R. Bassiri,⁴⁷ A. Basti,^{22,23} J. C. Batch,⁴⁴ C. Baune,⁹ M. Bawaj,^{48,40} M. Bazzan,^{49,50} B. Bécsy,⁵¹ C. Beer,⁹ M. Bejger,⁵² I. Belahcene,²⁶ A. S. Bell,⁴³ B. K. Berger,¹ G. Bergmann,⁹ C. P. L. Berry,⁵³ D. Bersanetti,^{54,55} A. Bertolini,¹³ J. Betzwieser,⁶ S. Bhagwat,⁴¹ R. Bhandare,⁵⁶ I. A. Bilenko,⁵⁷ G. Billingsley,¹ C. R. Billman,⁵ J. Birch,⁶ R. Birney,⁵⁸ O. Birnholtz,⁹ S. Biscans,¹⁴ A. Bisht,²¹ M. Bitossi,^{28,23} C. Biwer,⁴¹ M. A. Bizouard,²⁶ J. K. Blackburn,¹ J. Blackman,⁵⁹ C. D. Blair,⁶⁰ D. G. Blair,⁶⁰ R. M. Blair,⁴⁴ S. Bloemen,⁶¹ O. Bock,⁹ N. Bode,⁹ M. Boer,⁶² G. Bogaert,⁶² A. Bohe,³⁴ F. Bondu,⁶³ R. Bonnand,⁷ B. A. Boom,¹³ R. Bork,¹ V. Boschi,^{22,23} S. Bose,^{64,18} Y. Bouffanais,³⁵ A. Bozzi,²⁸ C. Bradaschia,²³ P. R. Brady,²⁰ V. B. Braginsky,^{57,†} M. Branchesi,^{65,66} J. E. Brau,⁶⁷ T. Briant,⁶⁸ A. Brillet,⁶² M. Brinkmann,⁹ V. Brisson,²⁶ P. Brockill,²⁰ J. E. Broida,⁶⁹ A. F. Brooks,¹ D. A. Brown,⁴¹ D. D. Brown,⁵³ N. M. Brown,¹⁴ S. Brunett,¹ C. C. Buchanan,² A. Buikema,¹⁴ T. Bulik,⁷⁰ H. J. Bulten,^{71,13} A. Buonanno,^{34,72} D. Buskulic,⁷ C. Buy,³⁵ R. L. Byer,⁴⁷ M. Cabero,⁹ L. Cadonati,⁷³ G. Cagnoli,^{25,74} C. Cahillane,¹ J. Calderón Bustillo,⁷³ T. A. Callister,¹ E. Calloni,^{75,4} J. B. Camp,⁷⁶ M. Canepa,^{54,55} P. Canizares,⁶¹ K. C. Cannon,⁷⁷ H. Cao,⁷⁸ J. Cao,⁷⁹ C. D. Capano,⁹ E. Capocasa,³⁵ F. Carbognani,²⁸ S. Caride,⁸⁰ M. F. Carney,⁸¹ J. Casanueva Diaz,²⁶ C. Casentini,^{30,17} S. Caudill,²⁰ M. Cavaglià,¹⁰ F. Cavalier,²⁶ R. Cavalieri,²⁸ G. Cella,²³ C. B. Cepeda,¹ L. Cerboni Baiardi,^{65,66} G. Cerretani,^{22,23} E. Cesarini,^{30,17} S. J. Chamberlin,⁸² M. Chan,⁴³ S. Chao,⁸³ P. Charlton,⁸⁴ E. Chassande-Mottin,³⁵ D. Chatterjee,²⁰ K. Chatziioannou,⁸⁵ B. D. Cheeseboro,^{37,38} H. Y. Chen,⁸⁶ Y. Chen,⁵⁹ H.-P. Cheng,⁵ A. Chincarini,⁵⁵ A. Chiummo,²⁸ T. Chmiel,⁸¹ H. S. Cho,⁸⁷ M. Cho,⁷² J. H. Chow,²⁴ N. Christensen,^{69,62} Q. Chu,⁶⁰ A. J. K. Chua,¹² S. Chua,⁶⁸ A. K. W. Chung,⁸⁸ S. Chung,⁶⁰ G. Ciani,⁵ R. Ciolfi,^{89,90} C. E. Cirelli,⁴⁷ A. Cirone,^{54,55} F. Clara,⁴⁴ J. A. Clark,⁷³ F. Cleva,⁶² C. Cocchieri,¹⁰ E. Coccia,^{16,17} P.-F. Cohadon,⁶⁸ A. Colla,^{91,32} C. G. Collette,⁹² L. R. Cominsky,⁹³ M. Constancio Jr.,¹⁵ L. Conti,⁵⁰ S. J. Cooper,⁵³ P. Corban,⁶ T. R. Corbitt,² K. R. Corley,⁴⁶ N. Cornish,⁹⁴ A. Corsi,⁸⁰ S. Cortese,²⁸ C. A. Costa,¹⁵ M. W. Coughlin,⁶⁹ S. B. Coughlin,^{95,96} J.-P. Coulon,⁶² S. T. Countryman,⁴⁶ P. Couvares,¹ P. B. Covas,⁹⁷ E. E. Cowan,⁷³ D. M. Coward,⁶⁰ M. J. Cowart,⁶ D. C. Coyne,¹ R. Coyne,⁸⁰ J. D. E. Creighton,²⁰ T. D. Creighton,⁹⁸ J. Cripe,² S. G. Crowder,⁹⁹ T. J. Cullen,²⁷ A. Cumming,⁴³ L. Cunningham,⁴³ E. Cuoco,²⁸ T. Dal Canton,⁷⁶ S. L. Danilishin,^{21,9} S. D'Antonio,¹⁷ K. Danzmann,^{21,9} A. Dasgupta,¹⁰⁰ C. F. Da Silva Costa,⁵ V. Dattilo,²⁸ I. Dave,⁵⁶ M. Davier,²⁶ D. Davis,⁴¹ E. J. Daw,¹⁰¹ B. Day,⁷³ S. De,⁴¹ D. DeBra,⁴⁷ E. Deelman,¹⁰² J. Degallaix,²⁵ M. De Laurentis,^{75,4} S. Deléglise,⁶⁸ W. Del Pozzo,^{53,22,23} T. Denker,⁹ T. Dent,⁹ V. Dergachev,³⁴ R. De Rosa,^{75,4} R. T. DeRosa,⁶ R. DeSalvo,¹⁰³ J. Devenson,⁵⁸ R. C. Devine,^{37,38} S. Dhurandhar,¹⁸ M. C. Díaz,⁹⁸ L. Di Fiore,⁴ M. Di Giovanni,^{104,90} T. Di Girolamo,^{75,4,46} A. Di Lieto,^{22,23} S. Di Pace,^{91,32} I. Di Palma,^{91,32} F. Di Renzo,^{22,23} Z. Doctor,⁸⁶ V. Dolique,²⁵ F. Donovan,¹⁴ K. L. Dooley,¹⁰ S. Doravari,⁹ I. Dorrington,⁹⁶ R. Douglas,⁴³ M. Dovalé Álvarez,⁵³ T. P. Downes,²⁰ M. Drago,⁹ R. W. P. Drever,^{1,‡} J. C. Driggers,⁴⁴ Z. Du,⁷⁹ M. Ducrot,⁷ J. Duncan,⁹⁵ S. E. Dwyer,⁴⁴ T. B. Edo,¹⁰¹ M. C. Edwards,⁶⁹ A. Effler,⁶ H.-B. Eggenstein,⁹ P. Ehrens,¹ J. Eichholz,¹ S. S. Eikenberry,⁵ R. A. Eisenstein,¹⁴ R. C. Essick,¹⁴ Z. B. Etienne,^{37,38} T. Etzel,¹ M. Evans,¹⁴ T. M. Evans,⁶ M. Factourovich,⁴⁶ V. Fafone,^{30,17,16} H. Fair,⁴¹ S. Fairhurst,⁹⁶ X. Fan,⁷⁹ S. Farinon,⁵⁵ B. Farr,⁸⁶ W. M. Farr,⁵³ E. J. Fauchon-Jones,⁹⁶ M. Favata,¹⁰⁵ M. Fays,⁹⁶ H. Fehrmann,⁹ J. Feicht,¹ M. M. Fejer,⁴⁷ A. Fernandez-Galiana,¹⁴ I. Ferrante,^{22,23} E. C. Ferreira,¹⁵ F. Ferrini,²⁸ F. Fidecaro,^{22,23} I. Fiori,²⁸ D. Fiorucci,³⁵ R. P. Fisher,⁴¹ R. Flaminio,^{25,106} M. Fletcher,⁴³ H. Fong,⁸⁵ P. W. F. Forsyth,²⁴ S. S. Forsyth,⁷³ J.-D. Fournier,⁶² S. Frasca,^{91,32} F. Frasconi,²³ Z. Frei,⁵¹ A. Freise,⁵³ R. Frey,⁶⁷ V. Frey,²⁶ E. M. Fries,¹ P. Fritschel,¹⁴ V. V. Frolov,⁶ P. Fulda,^{5,76} M. Fyffe,⁶ H. Gabbard,⁹ M. Gabel,¹⁰⁷ B. U. Gadre,¹⁸ S. M. Gaebel,⁵³ J. R. Gair,¹⁰⁸ L. Gammaitoni,³⁹ M. R. Ganija,⁷⁸ S. G. Gaonkar,¹⁸ F. Garufi,^{75,4} S. Gaudio,³³ G. Gaur,¹⁰⁹ V. Gayathri,¹¹⁰ N. Gehrels,^{76,§} G. Gemme,⁵⁵ E. Genin,²⁸ A. Gennai,²³ D. George,¹¹ J. George,⁵⁶ L. Gergely,¹¹¹ V. Germain,⁷ S. Ghonge,⁷³ Abhirup Ghosh,¹⁹ Archisman Ghosh,^{19,13} S. Ghosh,^{61,13} J. A. Giaime,^{2,6} K. D. Giardina,⁶ A. Giazotto,²³ K. Gill,³³ L. Glover,¹⁰³ E. Goetz,⁹ R. Goetz,⁵ S. Gomes,⁹⁶ G. González,² J. M. Gonzalez Castro,^{22,23} A. Gopakumar,¹¹² M. L. Gorodetsky,⁵⁷ S. E. Gossan,¹ M. Gosselin,²⁸ R. Gouaty,⁷ A. Grado,^{113,4} C. Graef,⁴³ M. Granata,²⁵ A. Grant,⁴³ S. Gras,¹⁴ C. Gray,⁴⁴ G. Greco,^{65,66} A. C. Green,⁵³ P. Groot,⁶¹ H. Grote,⁹ S. Grunewald,³⁴ P. Gruning,²⁶ G. M. Guidi,^{65,66} X. Guo,⁷⁹ A. Gupta,⁸² M. K. Gupta,¹⁰⁰ K. E. Gushwa,¹ E. K. Gustafson,¹ R. Gustafson,¹¹⁴ B. R. Hall,⁶⁴

E. D. Hall,¹ G. Hammond,⁴³ M. Haney,¹¹² M. M. Hanke,⁹ J. Hanks,⁴⁴ C. Hanna,⁸² M. D. Hannam,⁹⁶ O. A. Hannuksela,⁸⁸ J. Hanson,⁶ T. Hardwick,² J. Harms,^{65,66} G. M. Harry,¹¹⁵ I. W. Harry,³⁴ M. J. Hart,⁴³ C.-J. Haster,⁸⁵ K. Haughian,⁴³ J. Healy,¹¹⁶ A. Heidmann,⁶⁸ M. C. Heintze,⁶ H. Heitmann,⁶² P. Hello,²⁶ G. Hemming,²⁸ M. Hendry,⁴³ I. S. Heng,⁴³ J. Hennig,⁴³ J. Henry,¹¹⁶ A. W. Heptonstall,¹ M. Heurs,^{9,21} S. Hild,⁴³ D. Hoak,²⁸ D. Hofman,²⁵ K. Holt,⁶ D. E. Holz,⁸⁶ P. Hopkins,⁹⁶ C. Horst,²⁰ J. Hough,⁴³ E. A. Houston,⁴³ E. J. Howell,⁶⁰ Y. M. Hu,⁹ E. A. Huerta,¹¹ D. Huet,²⁶ B. Hughey,³³ S. Husa,⁹⁷ S. H. Huttner,⁴³ T. Huynh-Dinh,⁶ N. Indik,⁹ D. R. Ingram,⁴⁴ R. Inta,⁸⁰ G. Intini,^{91,32} H. N. Isa,⁴³ J.-M. Isac,⁶⁸ M. Isi,¹ B. R. Iyer,¹⁹ K. Izumi,⁴⁴ T. Jacqmin,⁶⁸ K. Jani,⁷³ P. Jaranowski,¹¹⁷ S. Jawahar,¹¹⁸ F. Jiménez-Forteza,⁹⁷ W. W. Johnson,² N. K. Johnson-McDaniel,¹⁹ D. I. Jones,¹¹⁹ R. Jones,⁴³ R. J. G. Jonker,¹³ L. Ju,⁶⁰ J. Junker,⁹ C. V. Kalaghatgi,⁹⁶ V. Kalogera,⁹⁵ S. Kandhasamy,⁶ G. Kang,³⁶ J. B. Kanner,¹ S. Karki,⁶⁷ K. S. Karvinen,⁹ M. Kasprzack,² M. Katolik,¹¹ E. Katsavounidis,¹⁴ W. Katzman,⁶ S. Kaufer,²¹ K. Kawabe,⁴⁴ F. Kéfélian,⁶² D. Keitel,⁴³ A. J. Kemball,¹¹ R. Kennedy,¹⁰¹ C. Kent,⁹⁶ J. S. Key,¹²⁰ F. Y. Khalili,⁵⁷ I. Khan,^{16,17} S. Khan,⁹ Z. Khan,¹⁰⁰ E. A. Khazanov,¹²¹ N. Kijbunchoo,⁴⁴ Chunglee Kim,¹²² J. C. Kim,¹²³ W. Kim,⁷⁸ W. S. Kim,¹²⁴ Y.-M. Kim,^{87,122} S. J. Kimbrell,⁷³ E. J. King,⁷⁸ P. J. King,⁴⁴ R. Kirchhoff,⁹ J. S. Kissel,⁴⁴ L. Kleybolte,³¹ S. Klimenko,⁵ P. Koch,⁹ S. M. Koehlenbeck,⁹ S. Koley,¹³ V. Kondrashov,¹ A. Kontos,¹⁴ M. Korobko,³¹ W. Z. Korth,¹ I. Kowalska,⁷⁰ D. B. Kozak,¹ C. Krämer,⁹ V. Kringel,⁹ B. Krishnan,⁹ A. Królak,^{125,126} G. Kuehn,⁹ P. Kumar,⁸⁵ R. Kumar,¹⁰⁰ S. Kumar,¹⁹ L. Kuo,⁸³ A. Kutynia,¹²⁵ S. Kwang,²⁰ B. D. Lackey,³⁴ K. H. Lai,⁸⁸ M. Landry,⁴⁴ R. N. Lang,²⁰ J. Lange,¹¹⁶ B. Lantz,⁴⁷ R. K. Lanza,¹⁴ A. Lartaux-Vollard,²⁶ P. D. Lasky,¹²⁷ M. Laxen,⁶ A. Lazzarini,¹ C. Lazzaro,⁵⁰ P. Leaci,^{91,32} S. Leavey,⁴³ C. H. Lee,⁸⁷ H. K. Lee,¹²⁸ H. M. Lee,¹²² H. W. Lee,¹²³ K. Lee,⁴³ J. Lehmann,⁹ A. Lenon,^{37,38} M. Leonardi,^{104,90} N. Leroy,²⁶ N. Letendre,⁷ Y. Levin,¹²⁷ T. G. F. Li,⁸⁸ A. Libson,¹⁴ T. B. Littenberg,¹²⁹ J. Liu,⁶⁰ R. K. L. Lo,⁸⁸ N. A. Lockerbie,¹¹⁸ L. T. London,⁹⁶ J. E. Lord,⁴¹ M. Lorenzini,^{16,17} V. Lorette,¹³⁰ M. Lormand,⁶ G. Losurdo,²³ J. D. Lough,^{9,21} G. Lovelace,²⁷ H. Lück,^{21,9} D. Lumaca,^{30,17} A. P. Lundgren,⁹ R. Lynch,¹⁴ Y. Ma,⁵⁹ S. Macfoy,⁵⁸ B. Machenschalk,⁹ M. MacInnis,¹⁴ D. M. Macleod,² I. Magaña Hernandez,⁸⁸ F. Magaña-Sandoval,⁴¹ L. Magaña Zertuche,⁴¹ R. M. Magee,⁸² E. Majorana,³² I. Maksimovic,¹³⁰ N. Man,⁶² V. Mandic,⁴² V. Mangano,⁴³ G. L. Mansell,²⁴ M. Manske,²⁰ M. Mantovani,²⁸ F. Marchesoni,^{48,40} F. Marion,⁷ S. Márka,⁴⁶ Z. Márka,⁴⁶ C. Markakis,¹¹ A. S. Markosyan,⁴⁷ E. Maros,¹ F. Martelli,^{65,66} L. Martellini,⁶² I. W. Martin,⁴³ D. V. Martynov,¹⁴ J. N. Marx,¹ K. Mason,¹⁴ A. Masserot,⁷ T. J. Massinger,¹ M. Masso-Reid,⁴³ S. Mastrogiovanni,^{91,32} A. Matas,⁴² F. Matichard,¹⁴ L. Matone,⁴⁶ N. Mavalvala,¹⁴ R. Mayani,¹⁰² N. Mazumder,⁶⁴ R. McCarthy,⁴⁴ D. E. McClelland,²⁴ S. McCormick,⁶ L. McCuller,¹⁴ S. C. McGuire,¹³¹ G. McIntyre,¹ J. McIver,¹ D. J. McManus,²⁴ T. McRae,²⁴ S. T. McWilliams,^{37,38} D. Meacher,⁸² G. D. Meadors,^{34,9} J. Meidam,¹³ E. Mejuto-Villa,⁸ A. Melatos,¹³² G. Mendell,⁴⁴ R. A. Mercer,²⁰ E. L. Merilh,⁴⁴ M. Merzougui,⁶² S. Meshkov,¹ C. Messenger,⁴³ C. Messick,⁸² R. Metzdrorff,⁶⁸ P. M. Meyers,⁴² F. Mezzani,^{32,91} H. Miao,⁵³ C. Michel,²⁵ H. Middleton,⁵³ E. E. Mikhailov,¹³³ L. Milano,^{75,4} A. L. Miller,⁵ A. Miller,^{91,32} B. B. Miller,⁹⁵ J. Miller,¹⁴ M. Millhouse,⁹⁴ O. Minazzoli,⁶² Y. Minenkov,¹⁷ J. Ming,³⁴ C. Mishra,¹³⁴ S. Mitra,¹⁸ V. P. Mitrofanov,⁵⁷ G. Mitselmakher,⁵ R. Mittleman,¹⁴ A. Moggi,²³ M. Mohan,²⁸ S. R. P. Mohapatra,¹⁴ M. Montani,^{65,66} B. C. Moore,¹⁰⁵ C. J. Moore,¹² D. Moraru,⁴⁴ G. Moreno,⁴⁴ S. R. Morris,⁹⁸ B. Mours,⁷ C. M. Mow-Lowry,⁵³ G. Mueller,⁵ A. W. Muir,⁹⁶ Arunava Mukherjee,⁹ D. Mukherjee,²⁰ S. Mukherjee,⁹⁸ N. Mukund,¹⁸ A. Mullavey,⁶ J. Munch,⁷⁸ E. A. M. Muniz,⁴¹ P. G. Murray,⁴³ K. Napier,⁷³ I. Nardecchia,^{30,17} L. Naticchioni,^{91,32} R. K. Nayak,¹³⁵ G. Nelemans,^{61,13} T. J. N. Nelson,⁶ M. Neri,^{54,55} M. Nery,⁹ A. Neunzert,¹¹⁴ J. M. Newport,¹¹⁵ G. Newton,^{43,||} K. K. Y. Ng,⁸⁸ T. T. Nguyen,²⁴ D. Nichols,⁶¹ A. B. Nielsen,⁹ S. Nissanke,^{61,13} A. Nitz,⁹ A. Noack,⁹ F. Nocera,²⁸ D. Nolting,⁶ M. E. N. Normandin,⁹⁸ L. K. Nuttall,⁴¹ J. Oberling,⁴⁴ E. Ochsner,²⁰ E. Oelker,¹⁴ G. H. Ogin,¹⁰⁷ J. J. Oh,¹²⁴ S. H. Oh,¹²⁴ F. Ohme,⁹ M. Oliver,⁹⁷ P. Oppermann,⁹ Richard J. Oram,⁶ B. O'Reilly,⁶ R. Ormiston,⁴² L. F. Ortega,⁵ R. O'Shaughnessy,¹¹⁶ D. J. Ottaway,⁷⁸ H. Overmier,⁶ B. J. Owen,⁸⁰ A. E. Pace,⁸² J. Page,¹²⁹ M. A. Page,⁶⁰ A. Pai,¹¹⁰ S. A. Pai,⁵⁶ J. R. Palamos,⁶⁷ O. Palashov,¹²¹ C. Palomba,³² A. Pal-Singh,³¹ H. Pan,⁸³ B. Pang,⁵⁹ P. T. H. Pang,⁸⁸ C. Pankow,⁹⁵ F. Pannarale,⁹⁶ B. C. Pant,⁵⁶ F. Paoletti,²³ A. Paoli,²⁸ M. A. Papa,^{34,20,9} H. R. Paris,⁴⁷ W. Parker,⁶ D. Pascucci,⁴³ A. Pasqualetti,²⁸ R. Passaquieti,^{22,23} D. Passuello,²³ B. Patricelli,^{136,23} B. L. Pearlstone,⁴³ M. Pedraza,¹ R. Pedurand,^{25,137} L. Pekowsky,⁴¹ A. Pele,⁶ S. Penn,¹³⁸ C. J. Perez,⁴⁴ A. Perreca,^{1,104,90} L. M. Perri,⁹⁵ H. P. Pfeiffer,⁸⁵ M. Phelps,⁴³ O. J. Piccinni,^{91,32} M. Pichot,⁶² F. Piergiovanni,^{65,66} V. Pierro,⁸ G. Pillant,²⁸ L. Pinard,²⁵ I. M. Pinto,⁸ M. Pitkin,⁴³ R. Poggiani,^{22,23} P. Popolizio,²⁸ E. K. Porter,³⁵ A. Post,⁹ J. Powell,⁴³ J. Prasad,¹⁸ J. W. W. Pratt,³³ V. Predoi,⁹⁶ T. Prestegard,²⁰ M. Prijatelj,⁹ M. Principe,⁸ S. Privitera,³⁴ G. A. Prodi,^{104,90} L. G. Prokhorov,⁵⁷ O. Puncken,⁹ M. Punturo,⁴⁰ P. Puppo,³² M. Pürer,³⁴ H. Qi,²⁰ J. Qin,⁶⁰ S. Qiu,¹²⁷ V. Quetschke,⁹⁸ E. A. Quintero,¹ R. Quitzow-James,⁶⁷ F. J. Raab,⁴⁴ D. S. Rabeling,²⁴ H. Radkins,⁴⁴ P. Raffai,⁵¹ S. Raja,⁵⁶ C. Rajan,⁵⁶ M. Rakhmanov,⁹⁸ K. E. Ramirez,⁹⁸ P. Rapagnani,^{91,32} V. Raymond,³⁴ M. Razzano,^{22,23} J. Read,²⁷ T. Regimbau,⁶² L. Rei,⁵⁵

S. Reid,⁵⁸ D. H. Reitze,^{1,5} H. Rew,¹³³ S. D. Reyes,⁴¹ F. Ricci,^{91,32} P. M. Ricker,¹¹ S. Rieger,⁹ K. Riles,¹¹⁴ M. Rizzo,¹¹⁶ N. A. Robertson,^{1,43} R. Robie,⁴³ F. Robinet,²⁶ A. Rocchi,¹⁷ L. Rolland,⁷ J. G. Rollins,¹ V. J. Roma,⁶⁷ J. D. Romano,⁹⁸ R. Romano,^{3,4} C. L. Romel,⁴⁴ J. H. Romie,⁶ D. Rosińska,^{139,52} M. P. Ross,¹⁴⁰ S. Rowan,⁴³ A. Rüdiger,⁹ P. Ruggi,²⁸ K. Ryan,⁴⁴ M. Rynge,¹⁰² S. Sachdev,¹ T. Sadecki,⁴⁴ L. Sadeghian,²⁰ M. Sakellariadou,¹⁴¹ L. Salconi,²⁸ M. Saleem,¹¹⁰ F. Salemi,⁹ A. Samajdar,¹³⁵ L. Sammut,¹²⁷ L. M. Sampson,⁹⁵ E. J. Sanchez,¹ V. Sandberg,⁴⁴ B. Sandeen,⁹⁵ J. R. Sanders,⁴¹ B. Sassolas,²⁵ B. S. Sathyaprakash,^{82,96} P. R. Saulson,⁴¹ O. Sauter,¹¹⁴ R. L. Savage,⁴⁴ A. Sawadsky,²¹ P. Schale,⁶⁷ J. Scheuer,⁹⁵ E. Schmidt,³³ J. Schmidt,⁹ P. Schmidt,^{1,61} R. Schnabel,³¹ R. M. S. Schofield,⁶⁷ A. Schönbeck,³¹ E. Schreiber,⁹ D. Schuette,^{9,21} B. W. Schulte,⁹ B. F. Schutz,^{96,9} S. G. Schwalbe,³³ J. Scott,⁴³ S. M. Scott,²⁴ E. Seidel,¹¹ D. Sellers,⁶ A. S. Sengupta,¹⁴² D. Sentenac,²⁸ V. Sequino,^{30,17} A. Sergeev,¹²¹ D. A. Shaddock,²⁴ T. J. Shaffer,⁴⁴ A. A. Shah,¹²⁹ M. S. Shahriar,⁹⁵ L. Shao,³⁴ B. Shapiro,⁴⁷ P. Shawhan,⁷² A. Sheperd,²⁰ D. H. Shoemaker,¹⁴ D. M. Shoemaker,⁷³ K. Siellez,⁷³ X. Siemens,²⁰ M. Sieniawska,⁵² D. Sigg,⁴⁴ A. D. Silva,¹⁵ A. Singer,¹ L. P. Singer,⁷⁶ A. Singh,^{34,9,21} R. Singh,² A. Singhal,^{16,32} A. M. Sintes,⁹⁷ B. J. J. Slagmolen,²⁴ B. Smith,⁶ J. R. Smith,²⁷ R. J. E. Smith,¹ E. J. Son,¹²⁴ J. A. Sonnenberg,²⁰ B. Sorazu,⁴³ F. Sorrentino,⁵⁵ T. Souradeep,¹⁸ A. P. Spencer,⁴³ A. K. Srivastava,¹⁰⁰ A. Staley,⁴⁶ M. Steinke,⁹ J. Steinlechner,^{43,31} S. Steinlechner,³¹ D. Steinmeyer,^{9,21} B. C. Stephens,²⁰ S. P. Stevenson,⁵³ R. Stone,⁹⁸ K. A. Strain,⁴³ G. Stratta,^{65,66} S. E. Strigin,⁵⁷ R. Sturani,¹⁴³ A. L. Stuver,⁶ T. Z. Summerscales,¹⁴⁴ L. Sun,¹³² S. Sunil,¹⁰⁰ P. J. Sutton,⁹⁶ B. L. Swinkels,²⁸ M. J. Szczepańczyk,³³ M. Tacca,³⁵ D. Talukder,⁶⁷ D. B. Tanner,⁵ M. Tápai,¹¹¹ A. Taracchini,³⁴ J. A. Taylor,¹²⁹ R. Taylor,¹ T. Theeg,⁹ E. G. Thomas,⁵³ M. Thomas,⁶ P. Thomas,⁴⁴ K. A. Thorne,⁶ K. S. Thorne,⁵⁹ E. Thrane,¹²⁷ S. Tiwari,^{16,90} V. Tiwari,⁹⁶ K. V. Tokmakov,¹¹⁸ K. Toland,⁴³ M. Tonelli,^{22,23} Z. Tornasi,⁴³ C. I. Torrie,¹ D. Töyrä,⁵³ F. Travasso,^{28,40} G. Traylor,⁶ D. Trifirò,¹⁰ J. Trinastic,⁵ M. C. Tringali,^{104,90} L. Trozzo,^{145,23} K. W. Tsang,¹³ M. Tse,¹⁴ R. Tso,¹ D. Tuyenbayev,⁹⁸ K. Ueno,²⁰ D. Ugolini,¹⁴⁶ C. S. Unnikrishnan,¹¹² A. L. Urban,¹ S. A. Usman,⁹⁶ K. Vahi,¹⁰² H. Vahlbruch,²¹ G. Vajente,¹ G. Valdes,⁹⁸ M. Vallisneri,⁵⁹ N. van Bakel,¹³ M. van Beuzekom,¹³ J. F. J. van den Brand,^{71,13} C. Van Den Broeck,¹³ D. C. Vander-Hyde,⁴¹ L. van der Schaaf,¹³ J. V. van Heijningen,¹³ A. A. van Veggel,⁴³ M. Vardaro,^{49,50} V. Varma,⁵⁹ S. Vass,¹ M. Vasúth,⁴⁵ A. Vecchio,⁵³ G. Vedovato,⁵⁰ J. Veitch,⁵³ P. J. Veitch,⁷⁸ K. Venkateswara,¹⁴⁰ G. Venugopalan,¹ D. Verkindt,⁷ F. Vetranò,^{65,66} A. Viceré,^{65,66} A. D. Viets,²⁰ S. Vinciguerra,⁵³ D. J. Vine,⁵⁸ J.-Y. Vinet,⁶² S. Vitale,¹⁴ T. Vo,⁴¹ H. Vocca,^{39,40} C. Vorvick,⁴⁴ D. V. Voss,⁵ W. D. Vousden,⁵³ S. P. Vyatchanin,⁵⁷ A. R. Wade,¹ L. E. Wade,⁸¹ M. Wade,⁸¹ R. M. Wald,⁸⁶ R. Walet,¹³ M. Walker,² L. Wallace,¹ S. Walsh,²⁰ G. Wang,^{16,66} H. Wang,⁵³ J. Z. Wang,⁸² M. Wang,⁵³ Y.-F. Wang,⁸⁸ Y. Wang,⁶⁰ R. L. Ward,²⁴ J. Warner,⁴⁴ M. Was,⁷ J. Watchi,⁹² B. Weaver,⁴⁴ L.-W. Wei,^{9,21} M. Weinert,⁹ A. J. Weinstein,¹ R. Weiss,¹⁴ L. Wen,⁶⁰ E. K. Wessel,¹¹ P. Weßels,⁹ T. Westphal,⁹ K. Wette,⁹ J. T. Whelan,¹¹⁶ B. F. Whiting,⁵ C. Whittle,¹²⁷ D. Williams,⁴³ R. D. Williams,¹ A. R. Williamson,¹¹⁶ J. L. Willis,¹⁴⁷ B. Willke,^{21,9} M. H. Wimmer,^{9,21} W. Winkler,⁹ C. C. Wipf,¹ H. Wittel,^{9,21} G. Woan,⁴³ J. Woehler,⁹ J. Wofford,¹¹⁶ K. W. K. Wong,⁸⁸ J. Worden,⁴⁴ J. L. Wright,⁴³ D. S. Wu,⁹ G. Wu,⁶ W. Yam,¹⁴ H. Yamamoto,¹ C. C. Yancey,⁷² M. J. Yap,²⁴ Hang Yu,¹⁴ Haocun Yu,¹⁴ M. Yvert,⁷ A. Zadrożny,¹²⁵ M. Zanolin,³³ T. Zelenova,²⁸ J.-P. Zendri,⁵⁰ M. Zevin,⁹⁵ L. Zhang,¹ M. Zhang,¹³³ T. Zhang,⁴³ Y.-H. Zhang,¹¹⁶ C. Zhao,⁶⁰ M. Zhou,⁹⁵ Z. Zhou,⁹⁵ X. J. Zhu,⁶⁰ A. Zimmerman,⁸⁵ M. E. Zucker,^{1,14} and J. Zweizig¹

(LIGO Scientific and Virgo Collaboration)

¹LIGO, California Institute of Technology, Pasadena, California 91125, USA²Louisiana State University, Baton Rouge, Louisiana 70803, USA³Università di Salerno, Fisciano, I-84084 Salerno, Italy⁴INFN, Sezione di Napoli, Complesso Universitario di Monte S. Angelo, I-80126 Napoli, Italy⁵University of Florida, Gainesville, Florida 32611, USA⁶LIGO Livingston Observatory, Livingston, Louisiana 70754, USA⁷Laboratoire d'Annecy-le-Vieux de Physique des Particules (LAPP), Université Savoie Mont Blanc, CNRS/IN2P3, F-74941 Annecy, France⁸University of Sannio at Benevento, I-82100 Benevento, Italy and INFN, Sezione di Napoli, I-80100 Napoli, Italy⁹Albert-Einstein-Institut, Max-Planck-Institut für Gravitationsphysik, D-30167 Hannover, Germany¹⁰The University of Mississippi, University, Mississippi 38677, USA¹¹NCSA, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA¹²University of Cambridge, Cambridge CB2 1TN, United Kingdom¹³Nikhef, Science Park, 1098 XG Amsterdam, Netherlands

- ¹⁴*LIGO, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA*
- ¹⁵*Instituto Nacional de Pesquisas Espaciais, 12227-010 São José dos Campos, São Paulo, Brazil*
- ¹⁶*Gran Sasso Science Institute (GSSI), I-67100 L'Aquila, Italy*
- ¹⁷*INFN, Sezione di Roma Tor Vergata, I-00133 Roma, Italy*
- ¹⁸*Inter-University Centre for Astronomy and Astrophysics, Pune 411007, India*
- ¹⁹*International Centre for Theoretical Sciences, Tata Institute of Fundamental Research, Bengaluru 560089, India*
- ²⁰*University of Wisconsin-Milwaukee, Milwaukee, Wisconsin 53201, USA*
- ²¹*Leibniz Universität Hannover, D-30167 Hannover, Germany*
- ²²*Università di Pisa, I-56127 Pisa, Italy*
- ²³*INFN, Sezione di Pisa, I-56127 Pisa, Italy*
- ²⁴*OzGrav, Australian National University, Canberra, Australian Capital Territory 0200, Australia*
- ²⁵*Laboratoire des Matériaux Avancés (LMA), CNRS/IN2P3, F-69622 Villeurbanne, France*
- ²⁶*LAL, Univ. Paris-Sud, CNRS/IN2P3, Université Paris-Saclay, F-91898 Orsay, France*
- ²⁷*California State University Fullerton, Fullerton, California 92831, USA*
- ²⁸*European Gravitational Observatory (EGO), I-56021 Cascina, Pisa, Italy*
- ²⁹*Chennai Mathematical Institute, Chennai 603103, India*
- ³⁰*Università di Roma Tor Vergata, I-00133 Roma, Italy*
- ³¹*Universität Hamburg, D-22761 Hamburg, Germany*
- ³²*INFN, Sezione di Roma, I-00185 Roma, Italy*
- ³³*Embry-Riddle Aeronautical University, Prescott, Arizona 86301, USA*
- ³⁴*Albert-Einstein-Institut, Max-Planck-Institut für Gravitationsphysik, D-14476 Potsdam-Golm, Germany*
- ³⁵*APC, AstroParticule et Cosmologie, Université Paris Diderot, CNRS/IN2P3, CEA/Ifu, Observatoire de Paris, Sorbonne Paris Cité, F-75205 Paris Cedex 13, France*
- ³⁶*Korea Institute of Science and Technology Information, Daejeon 34141, Korea*
- ³⁷*West Virginia University, Morgantown, West Virginia 26506, USA*
- ³⁸*Center for Gravitational Waves and Cosmology, West Virginia University, Morgantown, West Virginia 26505, USA*
- ³⁹*Università di Perugia, I-06123 Perugia, Italy*
- ⁴⁰*INFN, Sezione di Perugia, I-06123 Perugia, Italy*
- ⁴¹*Syracuse University, Syracuse, New York 13244, USA*
- ⁴²*University of Minnesota, Minneapolis, Minnesota 55455, USA*
- ⁴³*SUPA, University of Glasgow, Glasgow G12 8QQ, United Kingdom*
- ⁴⁴*LIGO Hanford Observatory, Richland, Washington 99352, USA*
- ⁴⁵*Wigner RCP, RMKI, H-1121 Budapest, Konkoly Thege Miklós út 29-33, Hungary*
- ⁴⁶*Columbia University, New York, New York 10027, USA*
- ⁴⁷*Stanford University, Stanford, California 94305, USA*
- ⁴⁸*Università di Camerino, Dipartimento di Fisica, I-62032 Camerino, Italy*
- ⁴⁹*Università di Padova, Dipartimento di Fisica e Astronomia, I-35131 Padova, Italy*
- ⁵⁰*INFN, Sezione di Padova, I-35131 Padova, Italy*
- ⁵¹*MTA Eötvös University, "Lendület" Astrophysics Research Group, Budapest 1117, Hungary*
- ⁵²*Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences, 00-716, Warsaw, Poland*
- ⁵³*University of Birmingham, Birmingham B15 2TT, United Kingdom*
- ⁵⁴*Università degli Studi di Genova, I-16146 Genova, Italy*
- ⁵⁵*INFN, Sezione di Genova, I-16146 Genova, Italy*
- ⁵⁶*RRCAT, Indore MP 452013, India*
- ⁵⁷*Faculty of Physics, Lomonosov Moscow State University, Moscow 119991, Russia*
- ⁵⁸*SUPA, University of the West of Scotland, Paisley PA1 2BE, United Kingdom*
- ⁵⁹*Caltech CaRT, Pasadena, California 91125, USA*
- ⁶⁰*OzGrav, University of Western Australia, Crawley, Western Australia 6009, Australia*
- ⁶¹*Department of Astrophysics/IMAPP, Radboud University Nijmegen, P.O. Box 9010, 6500 GL Nijmegen, Netherlands*
- ⁶²*Artemis, Université Côte d'Azur, Observatoire Côte d'Azur, CNRS, CS 34229, F-06304 Nice Cedex 4, France*
- ⁶³*Institut de Physique de Rennes, CNRS, Université de Rennes 1, F-35042 Rennes, France*
- ⁶⁴*Washington State University, Pullman, Washington 99164, USA*
- ⁶⁵*Università degli Studi di Urbino "Carlo Bo," I-61029 Urbino, Italy*
- ⁶⁶*INFN, Sezione di Firenze, I-50019 Sesto Fiorentino, Firenze, Italy*
- ⁶⁷*University of Oregon, Eugene, Oregon 97403, USA*
- ⁶⁸*Laboratoire Kastler Brossel, UPMC-Sorbonne Universités, CNRS, ENS-PSL Research University, Collège de France, F-75005 Paris, France*
- ⁶⁹*Carleton College, Northfield, Minnesota 55057, USA*
- ⁷⁰*Astronomical Observatory Warsaw University, 00-478 Warsaw, Poland*
- ⁷¹*VU University Amsterdam, 1081 HV Amsterdam, Netherlands*

- ⁷²University of Maryland, College Park, Maryland 20742, USA
- ⁷³Center for Relativistic Astrophysics and School of Physics, Georgia Institute of Technology, Atlanta, Georgia 30332, USA
- ⁷⁴Université Claude Bernard Lyon 1, F-69622 Villeurbanne, France
- ⁷⁵Università di Napoli “Federico II,” Complesso Universitario di Monte S. Angelo, I-80126 Napoli, Italy
- ⁷⁶NASA Goddard Space Flight Center, Greenbelt, Maryland 20771, USA
- ⁷⁷RESCEU, University of Tokyo, Tokyo, 113-0033, Japan
- ⁷⁸OzGrav, University of Adelaide, Adelaide, South Australia 5005, Australia
- ⁷⁹Tsinghua University, Beijing 100084, China
- ⁸⁰Texas Tech University, Lubbock, Texas 79409, USA
- ⁸¹Kenyon College, Gambier, Ohio 43022, USA
- ⁸²The Pennsylvania State University, University Park, Pennsylvania 16802, USA
- ⁸³National Tsing Hua University, Hsinchu City, 30013 Taiwan, Republic of China
- ⁸⁴Charles Sturt University, Wagga Wagga, New South Wales 2678, Australia
- ⁸⁵Canadian Institute for Theoretical Astrophysics, University of Toronto, Toronto, Ontario M5S 3H8, Canada
- ⁸⁶University of Chicago, Chicago, Illinois 60637, USA
- ⁸⁷Pusan National University, Busan 46241, Korea
- ⁸⁸The Chinese University of Hong Kong, Shatin, NT, Hong Kong
- ⁸⁹INAF, Osservatorio Astronomico di Padova, Vicolo dell'Osservatorio 5, I-35122 Padova, Italy
- ⁹⁰INFN, Trento Institute for Fundamental Physics and Applications, I-38123 Povo, Trento, Italy
- ⁹¹Università di Roma “La Sapienza,” I-00185 Roma, Italy
- ⁹²Université Libre de Bruxelles, Brussels 1050, Belgium
- ⁹³Sonoma State University, Rohnert Park, California 94928, USA
- ⁹⁴Montana State University, Bozeman, Montana 59717, USA
- ⁹⁵Center for Interdisciplinary Exploration & Research in Astrophysics (CIERA), Northwestern University, Evanston, Illinois 60208, USA
- ⁹⁶Cardiff University, Cardiff CF24 3AA, United Kingdom
- ⁹⁷Universitat de les Illes Balears, IAC3–IEEC, E-07122 Palma de Mallorca, Spain
- ⁹⁸The University of Texas Rio Grande Valley, Brownsville, Texas 78520, USA
- ⁹⁹Bellevue College, Bellevue, Washington 98007, USA
- ¹⁰⁰Institute for Plasma Research, Bhat, Gandhinagar 382428, India
- ¹⁰¹The University of Sheffield, Sheffield S10 2TN, United Kingdom
- ¹⁰²University of Southern California Information Sciences Institute, Marina Del Rey, California 90292, USA
- ¹⁰³California State University, Los Angeles, 5151 State University Drive, Los Angeles, California 90032, USA
- ¹⁰⁴Università di Trento, Dipartimento di Fisica, I-38123 Povo, Trento, Italy
- ¹⁰⁵Montclair State University, Montclair, New Jersey 07043, USA
- ¹⁰⁶National Astronomical Observatory of Japan, 2-21-1 Osawa, Mitaka, Tokyo 181-8588, Japan
- ¹⁰⁷Whitman College, 345 Boyer Avenue, Walla Walla, Washington 99362 USA
- ¹⁰⁸School of Mathematics, University of Edinburgh, Edinburgh EH9 3FD, United Kingdom
- ¹⁰⁹University and Institute of Advanced Research, Gandhinagar Gujarat 382007, India
- ¹¹⁰IISER-TVM, CET Campus, Trivandrum Kerala 695016, India
- ¹¹¹University of Szeged, Dóm tér 9, Szeged 6720, Hungary
- ¹¹²Tata Institute of Fundamental Research, Mumbai 400005, India
- ¹¹³INAF, Osservatorio Astronomico di Capodimonte, I-80131, Napoli, Italy
- ¹¹⁴University of Michigan, Ann Arbor, Michigan 48109, USA
- ¹¹⁵American University, Washington, D.C. 20016, USA
- ¹¹⁶Rochester Institute of Technology, Rochester, New York 14623, USA
- ¹¹⁷University of Białystok, 15-424 Białystok, Poland
- ¹¹⁸SUPA, University of Strathclyde, Glasgow G1 1XQ, United Kingdom
- ¹¹⁹University of Southampton, Southampton SO17 1BJ, United Kingdom
- ¹²⁰University of Washington Bothell, 18115 Campus Way NE, Bothell, Washington 98011, USA
- ¹²¹Institute of Applied Physics, Nizhny Novgorod, 603950, Russia
- ¹²²Seoul National University, Seoul 08826, Korea
- ¹²³Inje University Gimhae, South Gyeongsang 50834, Korea
- ¹²⁴National Institute for Mathematical Sciences, Daejeon 34047, Korea
- ¹²⁵NCBJ, 05-400 Świerk-Otwock, Poland
- ¹²⁶Institute of Mathematics, Polish Academy of Sciences, 00656 Warsaw, Poland
- ¹²⁷OzGrav, School of Physics & Astronomy, Monash University, Clayton 3800, Victoria, Australia
- ¹²⁸Hanyang University, Seoul 04763, Korea
- ¹²⁹NASA Marshall Space Flight Center, Huntsville, Alabama 35811, USA
- ¹³⁰ESPCI, CNRS, F-75005 Paris, France

- ¹³¹*Southern University and A&M College, Baton Rouge, Louisiana 70813, USA*
¹³²*OzGrav, University of Melbourne, Parkville, Victoria 3010, Australia*
¹³³*College of William and Mary, Williamsburg, Virginia 23187, USA*
¹³⁴*Indian Institute of Technology Madras, Chennai 600036, India*
¹³⁵*IISER-Kolkata, Mohanpur, West Bengal 741252, India*
¹³⁶*Scuola Normale Superiore, Piazza dei Cavalieri 7, I-56126 Pisa, Italy*
¹³⁷*Université de Lyon, F-69361 Lyon, France*
¹³⁸*Hobart and William Smith Colleges, Geneva, New York 14456, USA*
¹³⁹*Janusz Gil Institute of Astronomy, University of Zielona Góra, 65-265 Zielona Góra, Poland*
¹⁴⁰*University of Washington, Seattle, Washington 98195, USA*
¹⁴¹*King's College London, University of London, London WC2R 2LS, United Kingdom*
¹⁴²*Indian Institute of Technology, Gandhinagar Ahmedabad Gujarat 382424, India*
¹⁴³*International Institute of Physics, Universidade Federal do Rio Grande do Norte, Natal RN 59078-970, Brazil*
¹⁴⁴*Andrews University, Berrien Springs, Michigan 49104, USA*
¹⁴⁵*Università di Siena, I-53100 Siena, Italy*
¹⁴⁶*Trinity University, San Antonio, Texas 78212, USA*
¹⁴⁷*Abilene Christian University, Abilene, Texas 79699, USA*

*Deceased, March 2016.

†Deceased, March 2017.

‡Deceased, February 2017.

§Deceased, December 2016.